

# SOLUTIONS

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**SOLUTIONS FOR UTS-15**  
**CBSE SAMPLE PAPERS**  
**(Umang Test Series)**

**A TEAM EFFORT FROM**  
**O.P. GUPTA**  
**SACHIN PANDEY**  
**VISHAL MINOCHA**



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UTS-15  
CBSE Sample Papers  
(Umang Test Series)

Date \_\_\_\_\_  
DELTA Pg No. \_\_\_\_\_

Section - A

By O.P. Gupta, Sachin Pandey, Vishal Minocha

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1. (c) 12

11. (b) 17

2. (d) both b & c

12. (a)  $7/2$

3. (d)  $x = 5, y = 3$

13. (c) 12

4. (c) 3

14. (b) 44 cm

5. (d) -18

15. (c) -2

6. (b)  $17/6$

16. (a) 0

7. (b) 6

17. (b)  $128 \text{ cm}^2$

8. (d) class mark

18. (b) 5 cm

9. (d)  $1/6$

19. (d) A false R true

10. (a) 2

20. (d) A false R true

(2)

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## Section - B

21.  $x = a, y = b$

$$x - y = 2$$

$$x + y = 4$$

$$a - b = 2$$

$$a + b = 4$$

$$2a = 6$$

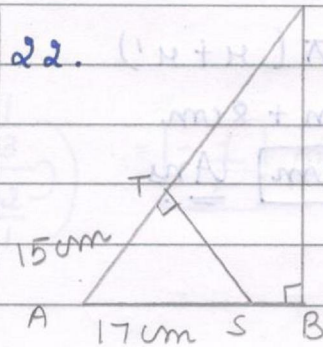
$$a = 3$$

$$3 - b = 2$$

$$-b = -1$$

$$b = 1 \text{ Ans.}$$

22.



$$TC = ?$$

$$\triangle ATS \sim \triangle ABC$$

$$(AA)$$

$$\angle A = \angle A \text{ (common)}$$

$$\angle T = \angle B \text{ (given)}$$

$$\frac{AT}{AB} = \frac{TS}{BC} \text{ (corres. sides of } \sim \Delta s)$$

$$\frac{15}{AB} = \frac{8}{16}$$

$$8AB = 240$$

$$AB = 30 \text{ cm}$$

$$\triangle ABC,$$

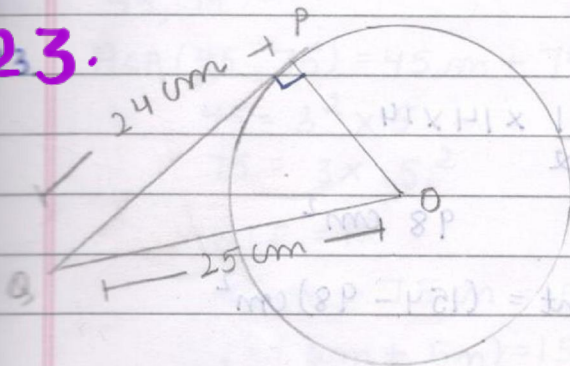
$$AC^2 = (30)^2 + 256$$

$$AC = 34 \text{ cm}$$

$$TSC = AC - TA = (34 - 15) \text{ cm}$$

$$19 \text{ cm} \text{ Ans.}$$

23.



$$OP = ?$$

$$OP \perp PQ \text{ (} \perp \text{ tangent at pt. of contact)}$$

$$\text{In } \triangle OPQ,$$

$$(25)^2 = (OP)^2 + 576$$

$$625 - 576 = (OP)^2$$

$$49 = (OP)^2$$

$$OP = 7 \text{ cm}$$

$$\text{radius} = 7 \text{ cm} \text{ Ans.}$$



③

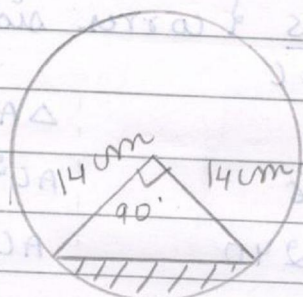
24.  $2\pi R = 2\pi r + 2\pi r'$  (given)

$2\pi R = 2\pi (r + r')$

$R = 6\text{ cm} + 8\text{ cm}$

$R = \boxed{14\text{ cm}}$  Ans

OR



area of segment = area of sector - area of  $\Delta$

(I) area of sector =  $\frac{90}{360} \times \frac{22}{7} \times 14 \times 14$

$\frac{1}{4} \times \frac{22}{7} \times 14 \times 14$

$154\text{ cm}^2$

(II) area of  $\Delta = \frac{1}{2} \times b \times h = \frac{1}{2} \times 14 \times 14$

$98\text{ cm}^2$

$\therefore$  area of segment =  $(154 - 98)\text{ cm}^2$

$\boxed{56\text{ cm}^2}$  Ans



4

25.  $\frac{\tan^2 30^\circ}{1 - \tan^2 60^\circ}$

$$\frac{\left(\frac{1}{\sqrt{3}}\right)^2}{1 - (\sqrt{3})^2} = \frac{\frac{1}{3}}{\frac{1-3}{1}} = \frac{\frac{1}{3}}{-2} = \boxed{-\frac{1}{6}} \text{ Ans}$$

OR.

$\tan A + \cot A = 3$  ;  $\tan^2 A + \cot^2 A = ?$   
s.b.s

$(\tan A + \cot A)^2 = 9$

$\tan^2 A + \cot^2 A + 2 \tan A \frac{1}{\tan A} = 9$

$\tan^2 A + \cot^2 A = \boxed{7} \text{ Ans}$

Section - C

26. 45, 75

$\text{HCF}(45, 75) = 45m + 75n$

$45 = 3^2 \times 5$

$75 = 3 \times 5^2$

$\text{HCF} = 15$

$45m + 75n = 15$

$15(3m + 5n) = 15$

$3m + 5n = 1$

$m = 1 - 5n$

Ans :-

m	-3	-8	2
n	2	5	-1

5

$$27. \text{ product} = \alpha\beta = -\frac{1}{6}$$

$$\text{sum} = \alpha + \beta = +\frac{1}{6}$$

$$p(n) = k(n^2 - 5n + p)$$

$$k\left(n^2 - \frac{1}{6}n - \frac{1}{6}\right)$$

$$\frac{k(6n^2 - n - 1)}{6}$$

$$\frac{k}{6}(6n^2 - n - 1)$$

$$\frac{k}{6}[6n^2 - 3n + 2n - 1]$$

$$\frac{k}{6}[3n(n-1) + 1(2n-1)]$$

$$\alpha = \left[-\frac{1}{3}, \frac{1}{2}\right] \text{ Ans}$$



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28. Let the no's be  $x$  and  $y$

ATQ  $\frac{x}{y} = \frac{5}{6} \quad \text{--- (1)}$

$$\frac{x-8}{y-8} = \frac{4}{5}$$

$$5(x-8) = 4(y-8)$$

$$5x - 40 = 4y - 32$$

$$5x - 4y = -32 + 40$$

$$5x - 4y = 8$$

$$5x = 8 + 4y$$

$$x = \frac{8 + 4y}{5} \quad \text{--- (2)}$$

Equating  $x$  in (1)

$$\frac{8 + 4y}{5} = \frac{5}{6}$$

$$\frac{8 + 4y}{5} = \frac{5}{6}$$

$$25y = 6(8 + 4y)$$

$$25y - 24y = 48$$

$$\boxed{y = 48}$$

$$\boxed{x = 40} \quad \text{Ans}$$

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OR.

Let no. of students in hall A =  $x$   
" " " " B =  $y$

ATQ

$$(x-10) = (y+10)$$

$$(x+20) = 2(y-20)$$

$$x-10 = y+10$$

$$x-y = 20 \quad (1)$$

$$x-y = 20$$

$$(-) \quad x-2y = -60$$

$$\begin{array}{r} - \quad + \quad + \\ \hline y = 80 \end{array}$$

$$x-80 = 20$$

$$x = 100$$

$$y = 80$$

Ans-  $\therefore$  there are 100 students in hall A & 80 students in hall B.

29.  $(\sin \theta + \operatorname{cosec} \theta)^2 + (\cos \theta + \sec \theta)^2 = \tan^2 \theta + \cot^2 \theta + 7$   
LHS

$$\frac{\sin^2 \theta + \operatorname{cosec}^2 \theta + 2 \sin \theta \cdot \frac{1}{\sin \theta}}{\sin \theta} + \frac{\cos^2 \theta + \sec^2 \theta + 2 \cos \theta \cdot \frac{1}{\cos \theta}}{\cos \theta}$$

$$1+2+2 + (1+\tan^2 \theta) + (1+\cot^2 \theta)$$

$$7+\tan^2 \theta + \cot^2 \theta$$

$\therefore$  LHS = RHS

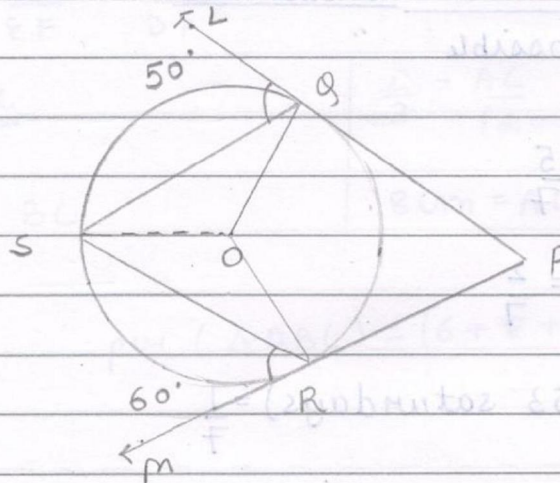
Hence, proved Ans



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30.



$$\angle QSR = ?$$

$$OQ \perp PL$$

$\{ r \perp \text{tangent at pt. of contact} \}$

$$OR \perp PM \{ " \}$$

$$\text{Now, } \angle OQL = \angle OQS + \angle SQL$$

$$90^\circ = \angle OQS + 50^\circ$$

$$\angle OQS = 40^\circ \text{ --- (1)}$$

$$\text{||ly } \angle ORM = 60^\circ + \angle ORS$$

$$90^\circ - 60^\circ = \angle ORS$$

$$30^\circ = \angle ORS \text{ --- (2)}$$

$\angle OQS = \angle OSQ$  &  $\angle S$  opp. to equal sides  $\{$

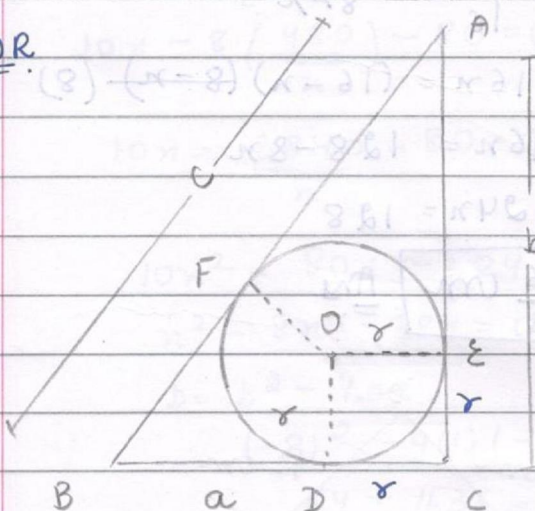
$$\text{||ly } \angle ORS = \angle OSR$$

$$\text{Also, } \angle QSR = \angle OSQ + \angle OSR$$

$$30^\circ + 40^\circ$$

$$= \boxed{70^\circ} \text{ Ans}$$

OR.



$$\text{T.P.} \Rightarrow H = \frac{a+b-c}{2}$$

Proof :-  $OEDC$  is a sq.

$\therefore CE = DC = H$  & tangents from same ext. pt  $\{$

$$\therefore AE = b - r$$

$$\text{||ly } BD = a - r$$

also,  $AE = AF$  & tangents from same ext pt  $\{$

$$BF = BD = \{ " \}$$

$$AB = AF + BF$$

$$c = b - r + a - r$$

$$c = b + a - 2r$$

$$\Rightarrow H = \frac{a+b-c}{2}$$

Hence, proved  
Ans



31.  $P(E) = \frac{\text{No. of favourable outcomes}}{\text{possible " "}}$

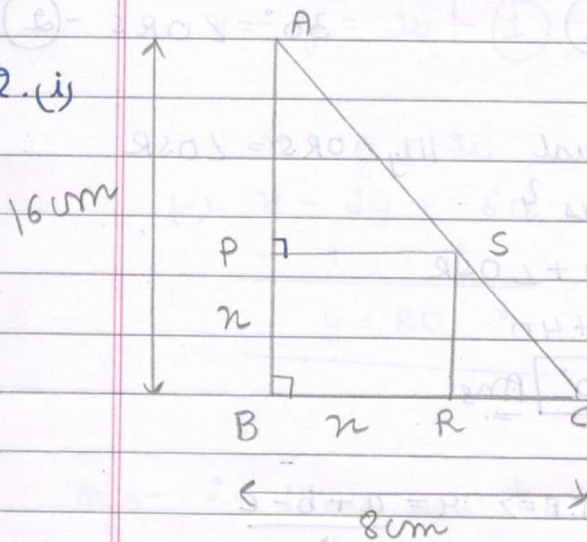
(i)  $P(52 \text{ sundays}) = \frac{5}{7}$

(ii)  $P(53 \text{ sundays}) = \frac{2}{7}$

(iii)  $P(52 \text{ sundays } 53 \text{ saturdays}) = \frac{1}{7}$

Section - D

32. (i)



$\triangle APS \sim \triangle ABC$  ( $\angle A A \angle$ )

$\angle A = \angle A$  (common)

$\angle APS = \angle ABC$  (each  $90^\circ$ )

$\frac{AP}{AB} = \frac{PS}{BC}$  (corres. sides of  $\sim$   $\triangle s$ )

$\frac{16-n}{16} = \frac{n}{8-n}$

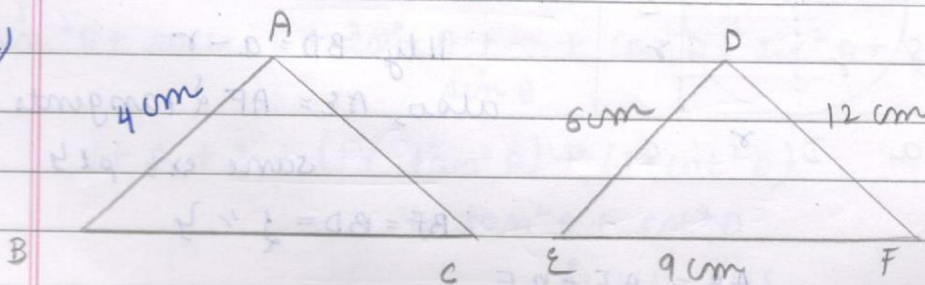
$16n = (16-n)(8-n)$

$16n = 128 - 8n$

$24n = 128$

$n = \frac{16 \text{ cm}}{3}$  Ans

(ii)



$\triangle ABC \sim \triangle DEF$



$$\frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF} \quad \text{Corresponding sides of } \sim \Delta s$$

$$\frac{2}{3} = \frac{BC}{9}$$

$$6 \text{ cm} = BC$$

$$\frac{2}{3} = \frac{AC}{12}$$

$$8 \text{ cm} = AC$$

$$\text{per}(\Delta ABC) = (6 + 8 + 4) \text{ cm}$$

$$= 18 \text{ cm} \quad \text{Ans.}$$

33. No. of students =  $n$

cost / student =  $y$

$$ny = 480$$

$$y = \frac{480}{n} - 1$$

$$(n-8)(y+10) = ny$$

$$ny + 10n - 8y - 80 = ny$$

$$10n - 8y - 80 = 0$$

$$10n - 8\left(\frac{480}{n}\right) - 80 = 0$$

$$10n - \frac{3840}{n} - 80 = 0$$

$$10n^2 - 80n - 3840 = 0$$

$$n^2 - 8n - 384 = 0$$

$$D = b^2 - 4ac$$

$$(-8)^2 - 4(1)(-384)$$

$$64 + 1536$$

$$\sqrt{D} = 40$$

$$\alpha = \frac{-b \pm \sqrt{D}}{2a} = \frac{8 \pm 40}{2} = 24$$

$\beta = -ve \rightarrow \text{rejected}$

no. of students

who attended

$$-24 - 8 = -32 \quad \text{Ans.}$$



OR

$$(1 + m^2)x^2 + 2mcx + c^2 - a^2 = 0$$

T.P.  $\Rightarrow c^2 = (1 + m^2)a^2$   
 $D = 0 ; b^2 - 4ac = 0$

$$(2mc)^2 - 4(1 + m^2)(c^2 - a^2) = 0$$

$$4m^2c^2 - 4[c^2 - a^2 + c^2m^2 - a^2m^2] = 0$$

$$4m^2c^2 - 4c^2 + 4a^2 - 4c^2m^2 + 4a^2m^2 = 0$$

$$-4c^2 + 4a^2 + 4a^2m^2 = 0$$

$$-4[c^2 - a^2 - a^2m^2] = 0$$

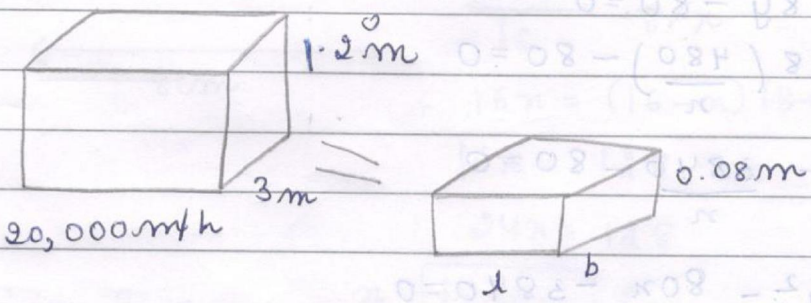
$$c^2 - a^2 - a^2m^2 = 0$$

$$c^2 = a^2 + a^2m^2$$

$$c^2 = a^2(1 + m^2)$$

Hence, proved Ans

34.



time =  $\frac{\text{area of field}}{\text{area of canal}} \Rightarrow \text{area of subside} = lbh$

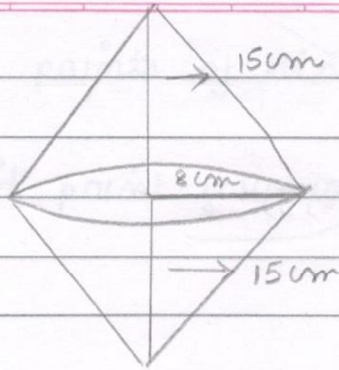
$$\frac{1}{3} = \frac{lb \times 0.08}{20,000 \times 3 \times 4}$$

$$300,000 \text{ m}^2$$

Ans



OR

TSA =  $2 \times$  CSA of cone

$$2 \times \pi r l$$

$$l^2 = r^2 + h^2$$

$$l^2 = 225 + 64$$

$$l = 17 \text{ cm}$$

$$2 \times \frac{22}{7} \times 8 \times 17 = \frac{5984}{7} \text{ cm}^2$$

$$\text{volume} = 2 \times \frac{1}{3} \pi r^2 h$$

$$2 \times \frac{1}{3} \times \frac{22}{7} \times 8 \times 8 \times 15 = \frac{14080}{7} \text{ cm}^3$$

Ans

	f	cf	
35. 0-5	12	12	Median = $1 + \frac{(n/2 - cf)}{f} \times h$
5-10	a	12 + a	
10-15	12	24 + a	Median class = 15-20 l = 15
15-20	15	39 + a	
20-25	b	39 + a + b	n/2 = 35 cf = 24 + a
25-30	6	45 + a + b	
30-35	6	51 + a + b	f = 15 h = 5
35-40	4	55 + a + b	
	<u>70</u>		

$$55 + a + b = 70$$

$$a + b = 15 \quad \text{--- (1)}$$

$$16 = 15 + \left[ \frac{35 - 24 - a}{15} \right] \times 5$$

$$3 = 11 - a$$

$$-8 = -a$$

$$\boxed{a = 8}$$

$$b = 15 - 8 = 7$$

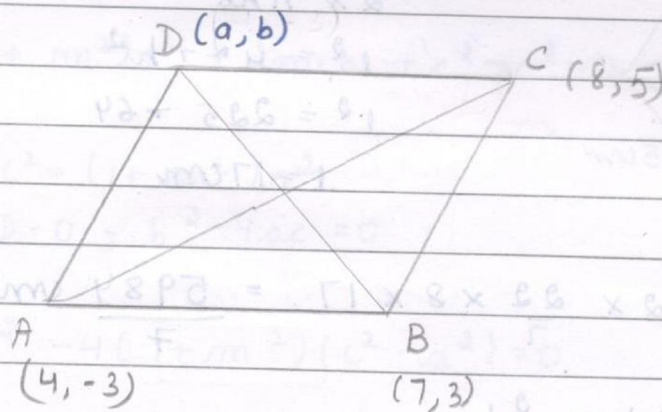
$$\boxed{b = 7} \quad \text{Ans}$$

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Section - E

36.



(i)

AC = ?

distance formula =  $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

$$\sqrt{(8 - 4)^2 + (5 - (-3))^2}$$

$$\sqrt{80} \text{ units} = 4\sqrt{5} \text{ units}$$

(ii)

BD = ?

$$\sqrt{(-1 - 7)^2 + (-1 - 3)^2} = \sqrt{(-8)^2 + (-4)^2}$$

$$4\sqrt{5} \text{ units}$$



(iii) mid points of diagonals are same in a ||gm

$$\text{mid point formula} = \left( \frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2} \right)$$

(iii) mid points of diagonals are same in a ||gm

$$\text{mid point formula} = \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

$$(3, 1) = \left( \frac{a+7}{2}, \frac{b+3}{2} \right)$$

$$\frac{a+7}{2} = 3$$

$$\frac{b+3}{2} = 1$$

$$a+7=6$$

$$b=-1$$

$$a = -1$$

$$D(a, b) = (-1, -1) \text{ Ans}$$

37.  $\pi [0.5, 1.0, 1.5, \dots]$

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

(i)  $a_7 = a_1 + 6d$

$$0.5 + 6(0.5)$$

$$0.5 + 3$$

$$3.5$$

$$\frac{22}{7} \times \frac{35}{10} = \boxed{11m}$$

(ii)  $a_{28} = a_1 + 27d$

$$0.5 + 27(0.5)$$

$$0.5 + 13.5$$

$$\frac{22}{7} \times 14$$

$$= \boxed{44m}$$

(iii)

$$S_{28} = 14 [1 + 13.5]$$

$$\frac{22}{7} \times 14 \times 14.5$$

$$\boxed{638m}$$

(iv)  $S_6 = \frac{6}{2} [2(0.5) + 5(0.5)]$

$$3[3.5]$$

$$10.5$$

$$\frac{22}{7} \times 10.5 = 33m$$

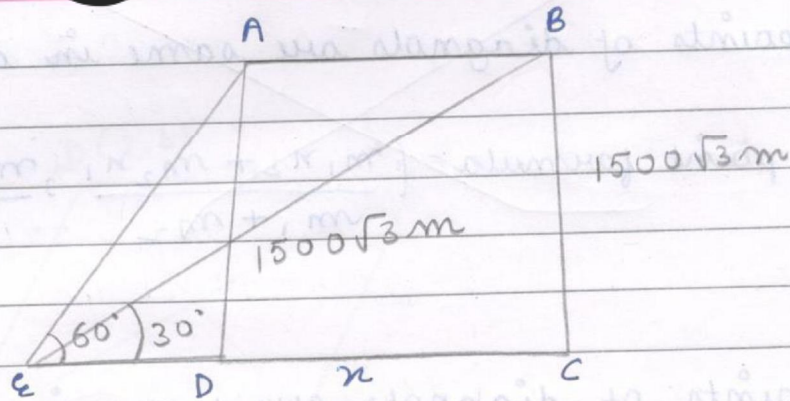
$$t = \frac{d}{s}$$

$$t = \frac{330}{5}$$

$$= \boxed{66s} \text{ Ans}$$



38.



(i) decreases

(ii) In  $\triangle ADE$ ,

$$\tan 60^\circ = \frac{1500\sqrt{3}}{ED}$$

$$\sqrt{3} = \frac{1500\sqrt{3}}{ED}$$

$$ED = 1500 \text{ m}$$

In  $\triangle BCE$ ,

$$\tan 30^\circ = \frac{1500\sqrt{3}}{1500 + x}$$

$$\frac{1}{\sqrt{3}} = \frac{1500\sqrt{3}}{1500 + x}$$

$$4500 = 1500 + x$$

$$3000 = x$$

$$s = \frac{d}{t}$$

$$s = \frac{3000}{15} = \boxed{200 \text{ m/s}}$$

(iii) 3000 m (solved above)

OR

(iv)  $EB = ?$ In  $\triangle EBC$ ,

$$\sin 30^\circ = \frac{1500\sqrt{3}}{EB}$$

$$\frac{1}{2} = \frac{1500\sqrt{3}}{EB}$$

$$EB = \boxed{3000\sqrt{3} \text{ m}} \quad \text{Ans}$$

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## Section-A

UTS-16

## CBSE Sample Papers (Umang Test Series)

1. (d) 435

2. (a) 0

3. (d)  $\sin 80^\circ$

4. (b)  $\sqrt{2}$

5. (a) 3:4

6. (b) 2

7. (b)  $25^\circ$

8. (d)  $\sqrt{7} + 2$

9. (b)  $3 - \sqrt{5}$

10. (c) 0.5

11. (c)  $AB + CD = AD + BC$

12. (d) 6.7 cm

13. (d)  $x^2 + 2x - 6$

14. (c) 1980 m

15. (d) 401.5 m

16. (a) 121 cm

17. (d) 0

18. (d) none of these

19. (a) Both are true, correct explanation

20. (d) A false, R true

By O.P. GUPTA,  
SACHIN PANDEY,  
VISHAL MINOCHA

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## Section - B

21. 
$$\begin{aligned} 2x + 3y &= 2xy \\ 4x + 3y &= 3xy \end{aligned} \quad \left. \begin{array}{l} \\ \end{array} \right\} \times 2$$

$$\begin{array}{r} 4x + 6y = 4xy \\ (-) 4x + 3y = 3xy \\ \hline 3y = xy \end{array}$$

$x = 3$

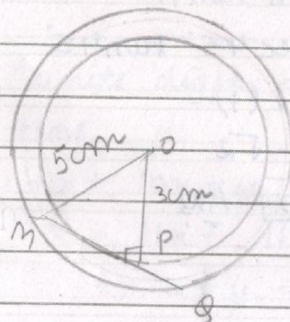
$$4(3) + 6y = 4(3)y$$

$$12 + 6y = 12y$$

$$12y = 6y$$

$y = 2$  Ans

23.



$$PM = ?$$

$$\text{In } \triangle OMP$$

$$\angle OPM = 90^\circ$$

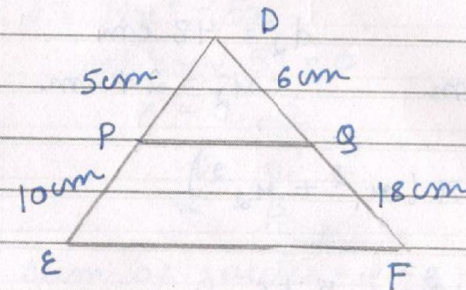
( $\perp$  tangent at point of contact)

$$25 = OP^2 + PM^2$$

$$16 = PM^2$$

$$4\text{cm} = PM$$

22.



$$PE = DE - DP = 10\text{cm}$$

$$\frac{DP}{PE} = \frac{5}{10} = \frac{1}{2}$$

$$\frac{DQ}{QF} = \frac{6}{18} = \frac{1}{3}$$

$$\text{As } \frac{DP}{PE} \neq \frac{DQ}{QF}$$

$$\therefore PQ \nparallel EF.$$

[ $\perp$  on chord from centre bisects

$$MQ = 2 \times 4 = 8\text{cm in the chord}]$$



24.  $d_1 = 20\text{cm}$   $d_2 = 48\text{cm}$   
 $r_1 = 10\text{cm}$   $r_2 = 24\text{cm}$

OR area of sector  $= \frac{\theta}{360} \pi R^2$

$$\pi R^2 = \pi (r_1^2 + r_2^2)$$

$$\frac{\theta}{360} \times 36 \times 36 = \frac{\pi 54}{10}$$

$$R^2 = 100 + 576$$

$$36 \times \theta = 540$$

$$R^2 = 676$$

$$\theta = 15^\circ$$

$$R = 26\text{cm}$$

$$\text{length of arc} = \frac{\theta}{360} \times 2\pi r$$

$$D = 26 \times 2 = \boxed{52\text{cm}} \text{ Ans}$$

$$\frac{15}{360} \times 2\pi \times 36$$

$$\boxed{3\pi\text{cm}} \text{ Ans}$$

25.  $\frac{(1 - \cos \theta)(1 + \cos \theta) \operatorname{cosec}^2 \theta}{(1 - \cos^2 \theta) \operatorname{cosec}^2 \theta}$   
 $\frac{\sin^2 \theta}{\sin^2 \theta}$

OR  $A = 45^\circ$

$$\sec A - \operatorname{cosec} A \tan A$$

$$\sec 45^\circ - \operatorname{cosec} 45^\circ \tan 45^\circ$$

$$\sqrt{2} - (\sqrt{2})(1)$$

$$\sqrt{2} - \sqrt{2}$$

$$= \boxed{1} \text{ Ans}$$

$$= \boxed{0} \text{ Ans}$$



name \_\_\_\_\_ roll no. \_\_\_\_\_ school \_\_\_\_\_  
 batch \_\_\_\_\_ ph. no. \_\_\_\_\_ sheet no. \_\_\_\_\_ date. \_\_\_\_\_

## Section - C

26. Sanju  $\rightarrow$  40 minutes  
 Suman  $\rightarrow$  32 minutes

$$40 = 2^3 \times 5$$

$$32 = 2^5$$

$$\text{LCM} = 2^5 \times 5$$

160 minutes

$\therefore$  they will meet again after 160 minutes.

$$\text{rounds by Sanju} = \frac{160}{40} = 4 \text{ rounds}$$

$$\text{" Suman} = \frac{160}{32} = 5 \text{ rounds } \underline{\text{Ans}}$$

$$27. 4x^2 - 5x$$

$$x(4x - 5) = 0$$

$$x = 0, \frac{5}{4}$$

$$\downarrow \quad \downarrow$$

$$\alpha \quad \beta$$

$$\text{Sum of zeroes} = \alpha + \beta = 0 + \frac{5}{4} = \frac{5}{4}$$

$$\text{product " } = \alpha\beta = (0)\left(\frac{5}{4}\right) = 0$$

$$-\frac{b}{a} = \frac{5}{4} ; \frac{c}{a} = 0$$

$$\therefore \alpha + \beta = -\frac{b}{a}, \alpha\beta = \frac{c}{a}$$

Hence, verified Ans

28. Let the units digit be  $x$

" tens " "  $y$

$$\text{ATQ } 10y + x + 10x + y = 88$$

$$11x + 11y = 88$$

$$x + y = 8 \quad \text{--- (1)}$$

Case 1:

$$x - y = 2 \quad \text{--- (2)}$$

$$+ \quad x + y = 8$$

$$\underline{2x = 10}$$

$$x = 5$$

$$y = 3$$

$$\text{No.} = \boxed{35}$$

Case 2:

$$x + y = 8$$

$$+ \quad -x + y = 2 \quad \text{--- (2)}$$

$$\underline{2y = 10}$$

$$y = 5$$

$$x = 3$$

$$\text{No.} = \boxed{53}$$

Ans -  $\therefore$  the no.

is either 35 or 53.



OR

Let the certain amount of money be ₹  $x$   
& other be ₹  $y$

ATQ  $\frac{12x}{100} + \frac{10y}{100} = 130$

$$12x + 10y = 13000$$

$$6x + 5y - 6500 = 0 \quad \text{--- (1)}$$

$$\frac{10x}{100} + \frac{12y}{100} = 134$$

$$10x + 12y = 13400$$

$$5x + 6y - 6700 = 0 \quad \text{--- (2)}$$

Multiplying (1) by 5 & (2) by 6

$$30x + 25y - 32500 = 0$$

$$(-) 30x + 36y - 40200 = 0$$

- - +

$$-11y + 7700 = 0$$

$$-11y = -7700$$

$$\boxed{y = 700} ; \boxed{x = 500} \quad \text{Ans}$$

$$29. \text{ T.P } \Rightarrow \sin^6 \alpha + \cos^6 \alpha + 3\sin^2 \alpha \cos^2 \alpha = 1$$

$$(\sin^2 \alpha + \cos^2 \alpha)^3 = 1^3$$
$$= 1$$

$$\sin^6 \alpha + \cos^6 \alpha + 3\sin^2 \alpha \cos^2 \alpha (1) = 1$$

$$\sin^6 \alpha + \cos^6 \alpha + 3\sin^2 \alpha \cos^2 \alpha = 1$$

using identity,  $(a+b)^3 = a^3 + b^3 + 3ab(a+b)$

Hence, proved Ans



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school \_\_\_\_\_

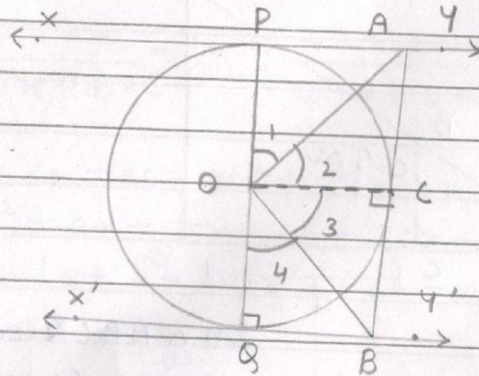
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ph. no. \_\_\_\_\_

sheet no. \_\_\_\_\_

date. \_\_\_\_\_

30.



Given:  $XY \parallel X'Y'$

T.P:  $\angle AOB = 90^\circ$

const.: Join OC

Proof: In  $\triangle OCB$  &  $\triangle OCB$

$OC = OC$  (radii)

$OB = OB$  (common)

$BC = BC$  (tangents from same ext. pt)

$\therefore \triangle OCB \cong \triangle OCB$  (SSS)  $\rightarrow \angle OCB$

$\therefore \angle 3 = \angle 4$  (cpct)

$\parallel$  by  $\angle 1 = \angle 2$

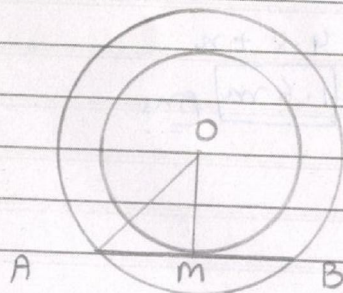
Now,  $\angle 1 + \angle 2 + \angle 3 + \angle 4 = 180^\circ$  (angles on a straight line)

$2(\angle 3 + \angle 4) = 180^\circ$

$\angle 3 + \angle 4 = 90^\circ$  i.e.  $\angle AOB = 90^\circ$

Hence, proved Ans

OR



Given: - (O, M)

T.P: -  $AM = BM$

Proof: -  $OM \perp AB$

( $M \perp$  tangent at pt. of contact)

$\therefore AM = BM$

( $\perp$  on chord from centre bisects the chord)

Hence, proved

31.  $P(4) = \frac{\text{No. of fav. outcomes}}{\text{" possible "}}$

(i)  $P(\text{divisible by } 2) = \frac{50}{100} = \frac{1}{2}$

(ii)  $P(\text{divisible by } 5) = \frac{20}{100} = \frac{1}{5}$

(iii)  $P(\text{divisible by } 2 \text{ \& } 5) = \frac{10}{100} = \frac{1}{10}$



# Section - D

$$32. (i) \triangle ABC \sim \triangle RQP \text{ (SSS)}$$

↓

$$\text{given that } \frac{AB}{RQ} = \frac{BC}{QP} = \frac{AC}{RP} = \frac{1}{2}$$

In  $\triangle ABC$ ,

$$60^\circ + 80^\circ + \angle C = 180^\circ \text{ [ASP of a } \triangle]$$

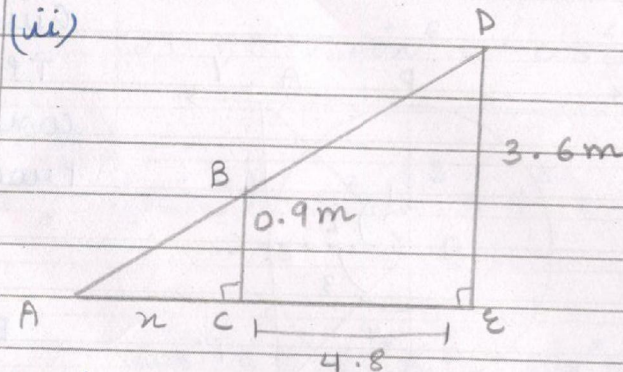
$$140^\circ + \angle C = 180^\circ$$

$$\angle C = 40^\circ$$

$$\angle C = \angle P \text{ [Corres. } \angle \text{ s of } \sim \Delta \text{ s]}$$

$$\boxed{\angle P = 40^\circ} \text{ Ans}$$

(ii)



$$\Delta = \frac{d}{t}$$

$$1.2 = \frac{d}{4}$$

$$4.8 \text{ m} = CE = \text{distance}$$

$$\frac{BC}{AB} = \frac{DE}{AE} \text{ (Corres. parts of } \sim \Delta \text{ s)}$$

$$\frac{0.9}{3.6} = \frac{n}{n+4.8}$$

$$4n = 4.8 + n$$

$$n = \boxed{1.6 \text{ m}} \text{ Ans}$$



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33.  $\frac{1}{n+a} + \frac{1}{n+b} = \frac{1}{c}$  ;  $S=0$   $P = -\frac{1}{2}(a^2+b^2)$

$$\frac{n+b+n+a}{(n+a)(n+b)} = \frac{1}{c} ; \frac{2n+a+b}{n^2+an+bn+ab} = \frac{1}{c}$$

$$2cn + ca + bc = n^2 + an + bn + ab$$

$$0 = n^2 + an + bn + ab - 2cn - ca - bc$$

$$n^2 + (a+b-2c)n + (ab-ca-bc) = 0$$

$$S=0 \quad -\frac{b}{a} = 0$$

$$b=0$$

$$a+b-2c=0$$

$$a+b=2c$$

$$c = \frac{a+b}{2}$$

$$\rightarrow P = \frac{c}{a}$$

$$\frac{ab-ac-bc}{1}$$

$$ab - (a+b)c$$

$$ab - (a+b)\left(\frac{a+b}{2}\right)$$

$$\frac{2ab - (a^2+b^2+2ab)}{2}$$

$$\frac{2ab - a^2 - b^2 - 2ab}{2}$$

$$-\frac{1}{2}(a^2+b^2)$$

Hence, proved  
Ans

OR  $pn^2 + 5n + 11 = 0$

put  $n=2$

$$p(2)^2 + 5(2) + 11 = 0$$

$$4p + 10 + 11 = 0$$

$$11 = -4p - 10 \quad \text{--- (1)}$$

put  $n = \frac{1}{2}$

$$p\left(\frac{1}{2}\right)^2 + 5\left(\frac{1}{2}\right) + 11 = 0$$

$$\frac{1}{4}p + \frac{5}{2} + 11 = 0$$

$$\frac{1}{4}p + \frac{5}{2} + (-4p - 10) = 0$$

$$\frac{1}{4}p + \frac{5}{2} - 4p - 10 = 0$$

$$\frac{p+10-16p-40}{4} = 0$$

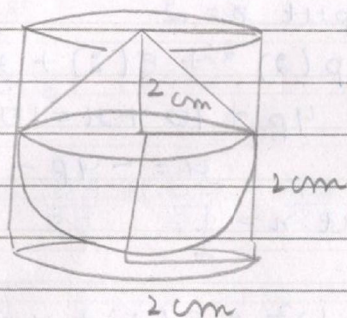
$$-15p = 30 \quad \boxed{p = -2}$$

$$11 = -4(-2) - 10 = 8 - 10$$

$$\boxed{11 = -2} \quad \text{Ans}$$



34.



volume of toy = volume of cone + vol. of hemisphere

$$\frac{1}{3} \pi r^2 h + \frac{2}{3} \pi r^3$$

$$\frac{1}{3} \pi r^2 [h + 2r]$$

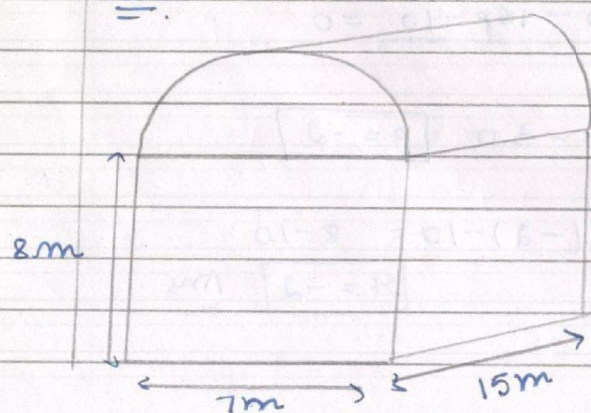
$$\frac{1}{3} \times \frac{22}{7} \times 2 \times 2 [2 + 4]$$

$$\frac{1}{3} \times \frac{22}{7} \times 2 \times 2 \times 6 = \boxed{25.1 \text{ cm}^3}$$

volume of cylinder =  $\pi r^2 h = \frac{314}{100} \times 4 \times 2 \times 2 = 50.24 \text{ cm}^3$

difference of volumes =  $50.24 - 25.1 = \boxed{25.1 \text{ cm}^3 \text{ Ans}}$

OR



(I) volume of air = volume of cuboid +  $\frac{1}{2}$  vol. of cylinder

$$(7)(15)(8) + \frac{1}{2} \left[ \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \times 15 \right]$$

$$840 + \frac{1}{2} \left[ \frac{1155}{2} \right]$$

$$840 + \frac{1155}{4} = 840 + 288.75 = \boxed{1128.75 \text{ m}^3}$$



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(II) volume by machinery =  $300\text{m}^3$

volume by 1 worker =  $0.08\text{m}^3$

" 20 " =  $0.08 \times 20 = 1.6\text{m}^3$

volume of air = volume of shed - (volume of machinery + volume of 20 workers)

$$1128.7 - (300 + 1.6)$$

$$1128.7 - 301.6$$

$$= \boxed{827.1\text{m}^3} \text{ Ans}$$

35.	Marks	cf	cf	$f_i$	$h_i$	$f_i h_i$
	0-10	50	35	3	5	15
	10-20	47	10-20	0	15	0
	20-30	47	20-30	8	25	200
	30-40	39	30-40	7	35	245
	40-50	32	40-50	4	45	180
	50-60	28	50-60	5	55	275
	60-70	23	60-70	5	65	325
	70-80	18	70-80	6	75	450
	80-90	12	80-90	5	85	425
	90-100	7	90-100	7	95	665
				50		2780

$$\text{Mean} = \frac{\sum f_i h_i}{\sum f_i}$$

$$= \frac{2780}{50}$$

$$\boxed{55.6}$$



### Section - E

36. (i) Batsman (3, 0) Extra cover (-7, -5)

$$\text{distance formula} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\sqrt{(-7-3)^2 + (-5-0)^2} = \sqrt{(-10)^2 + (-5)^2} = \sqrt{100+25} = \sqrt{125} = 5\sqrt{5} \text{ units}$$

(ii) third man (-5, 10) deep fine leg (5, 11)

$$\sqrt{(5+5)^2 + (11-10)^2}$$

$$\sqrt{10^2 + 1} = \sqrt{101} \text{ units}$$

(iii) Mid on (3, -8) wicket keeper (0, b)

$$\sqrt{117} = \sqrt{(0-3)^2 + (b+8)^2}$$

$$\sqrt{117} = \sqrt{9 + b^2 + 864 + 16b}$$

$$\sqrt{117} = \sqrt{9 + b^2 + 64 + 16b}$$

$$117 = 9 + b^2 + 64 + 16b$$

$$117 = b^2 + 16b + 73$$

$$0 = b^2 + 16b + 73 - 117$$

$$b^2 + 16b - 44$$

$$D = b^2 - 4ac$$

$$D = 80$$

$$\sqrt{D} = 4\sqrt{5}$$

$$\alpha, \beta = \frac{-b \pm \sqrt{D}}{2a}$$

$$= \frac{-16 \pm 4\sqrt{5}}{2} \text{ units}$$

Ans.



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(iii) OR C(-6, -1) B(0, -2), M(4, -3)

for the points to be collinear, area of  $\Delta$  must be 0 units

$$\begin{aligned} x_1 &= -6 & y_1 &= -1 \\ x_2 &= 0 & y_2 &= -2 \\ x_3 &= 4 & y_3 &= -3 \end{aligned}$$

$$A.O.\Delta = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$

$$\frac{1}{2} [(-6)(-1) + 0(-2) + (4)(-1)]$$

$$\frac{1}{2} [-6 + 0 + 4] = \frac{1}{2} [-2] = -1 = 1 \text{ units}$$

$\therefore$  they do not lie on a straight line. Ans

37.(i)  $a_4 = 1800$

$a_8 = 2600$

$a_1 + 3d = 1800$

(-)  $a_1 + 7d = 2600$

- - -

$+4d = +800$

$d = 200$

$a + 3(200) = 1800$

$a + 600 = 1800$

$a = 1200$

(ii)  $a_{12} = ?$

$a_1 + 11d$

$1200 + 11(200)$

$1200 + 2200$

$3400$  Ans



(iii)

$$S_{10} = ?$$

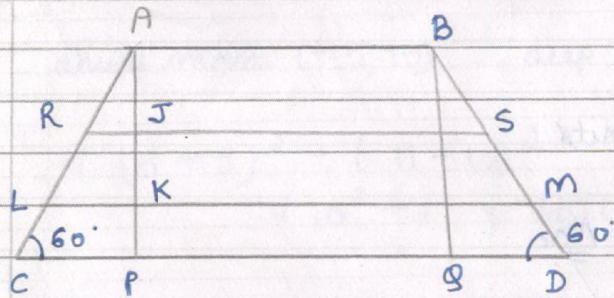
$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$5 [2400 + 9(200)]$$

$$5 [2400 + 1800]$$

$$5 [4200] = \boxed{21000} \text{ Ans}$$

38.



$$(i) \text{ In } \triangle APC, \sin 60^\circ = \frac{1.8}{AC}$$

$$\frac{\sqrt{3}}{2} = \frac{1.8}{AC}$$

$$5\sqrt{3} AC = 18$$

$$2.07 \text{ (approx.)}$$

$$\text{OR } S_n = 31200$$

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$31200 = \frac{n}{2} [2400 + (n-1)(200)]$$

$$62400 = n [2400 + 200n - 200]$$

$$62400 = 2400n + 200n^2 - 200n$$

$$62400 = 200n^2 + 2200n$$

$$0 = 200n^2 + 2200n - 62400$$

$$0 = 200(n^2 + 11n - 312)$$

$$0 = n^2 + 11n - 312$$

$$n^2 + 24n - 13n - 312$$

$$n(n+24) - 13(n+24)$$

$$13, -24$$

↓  
rejected

$$\text{Ans} - \boxed{13 \text{ years}}$$



(ii) AR = ?

In  $\triangle ACP$ ,

$$\tan 60^\circ = \frac{AP}{PC}$$

$$\sqrt{3} = \frac{1.8}{PC}$$

$$PC = 1.04$$

Now, in  $\triangle ARJ$  &  $\triangle ACP$ ,

$\angle A = \angle A$  (common)

$\angle J = \angle P$  (each  $90^\circ$ )

$\triangle ARJ \sim \triangle ACP$  (AA)

$$\frac{AR}{2.07} = \frac{0.6}{1.8} \quad (\text{corresponding sides of } \sim \triangle s)$$

$$3AR = 2.07$$

$$AR = \boxed{0.69 \text{ m}} \quad \text{Ans}$$

(iii) In  $\triangle ALK$ ,

$$\tan 60^\circ = \frac{1.2}{KL}$$

$$\sqrt{3} = \frac{1.2}{KL}$$

$$KL = \frac{1.2 \times \sqrt{3}}{\sqrt{3}} = \frac{1.2 \times 1.73}{1}$$

$$\frac{2.076}{3} = 0.692$$

$$LM = (0.692 \times 2) + 0.5$$

$$1.384 + 0.5$$

$$\boxed{1.884 \text{ m}}$$

OR

In  $\triangle ARJ$ ,

$$\tan 60^\circ = \frac{0.6}{RJ}$$

$$\sqrt{3} = \frac{0.6}{RJ} \quad RJ = \frac{0.6 \times \sqrt{3}}{\sqrt{3}}$$

$$\frac{0.6\sqrt{3}}{3}$$

$$= 0.2 \times 1.73$$

$$0.346$$

$$RS = (2 \times 0.346) + 0.5$$

$$\boxed{1.192 \text{ m}} \quad \text{Ans}$$

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Section A

UTS-17

①

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Ans 01. (a) 24 and 24

Ans 02. (b) 33

Ans 03. (b)  $K(x^2 + 2x - 15)$

Ans 04. (d)  $K = \text{no value}$

Ans 05. (d)  $\perp$

Ans 06. (d) RHS

Ans 07. (a)  $4/3$

Ans 08. (b) -1

Ans 09. (b) 30 units

Ans 10. (b) 8 units

Ans 11. (a) 462 sq. cm

Ans 12. (a) real and unequal

Ans 13. (b) 13 cm

Ans 14. (c)  $3 \text{ median} - 2 \text{ mean}$

Ans 15. (b) 4 units

Ans 16. (b)  $60^\circ$

Ans 17. (a)  $\frac{3}{8}$

Ans 18. (a) terminate after 3 decimal places.

Ans 19. (b) Both A and R are true and R is not the correct explanation of A.

Ans 20. (b) Both A and R are true and R is not the correct Explanation of A.



②

### Section B

Ans 21. Let  $\frac{2x}{3} + \frac{3y}{2} = 5 \rightarrow (1)$

$$\Rightarrow \frac{2x \times 2 + 3y \times 3}{6} = 5$$

$$\Rightarrow \frac{4x + 9y}{6} = 5$$

$$\Rightarrow 4x + 9y = 30 \rightarrow (1)$$

also,  $\frac{3x}{2} + \frac{2y}{3} = \frac{35}{6} \rightarrow (2)$

$$\Rightarrow \frac{3x \times 3 + 2y \times 2}{6} = \frac{35}{6}$$

$$\Rightarrow \frac{9x + 4y}{6} = \frac{35}{6}$$

$$\Rightarrow 9x + 4y = \frac{35 \times 6}{6}$$

$$\Rightarrow 9x + 4y = 35 \rightarrow (2)$$

multiply eq(1) by 4 and eq(2) by 9 we get,

$$\Rightarrow (4x + 9y = 30) \times 4, (9x + 4y = 35) \times 9$$

$$\Rightarrow 16x + 36y = 120 \quad \hookrightarrow (3), \quad 81x + 36y = 315 \quad \hookrightarrow (4)$$

On subtracting eq(3) from (4) we get,

$$\begin{array}{r} 81x + 36y = 315 \\ (-) 16x + 36y = 120 \\ \hline 65x + 0y = 195 \end{array}$$

$$65x = 195$$

$$x = \frac{195}{65} = 3 \Rightarrow \boxed{x=3}$$



(3)

using  $x=3$  in eq(1)

$$\Rightarrow 4(3) + 9y = 30$$

$$\Rightarrow 12 + 9y = 30$$

$$\Rightarrow 9y = 30 - 12$$

$$\Rightarrow 9y = 18$$

$$\Rightarrow y = \frac{18}{9} = 2$$

$$\Rightarrow \boxed{y=2}$$

Ans:  $x=3, y=2$

Ans 22. In  $\Delta POQ$ ,  $DE \parallel OQ$

$$\text{Hence, } \frac{PE}{EQ} = \frac{PD}{DO} \quad (\text{By BPT}) \rightarrow (1)$$

$$\text{Now, In } \Delta POR, \frac{PD}{DO} = \frac{PF}{FR} \quad (\text{by BPT}) \rightarrow (2)$$

On comparing eq(1) and (2)

$$\text{we get, } \frac{PE}{EQ} = \frac{PF}{FR}$$

$\rightarrow$  This implies that,  $EF \parallel QR$ . (by converse of BPT)

Ans 23. To prove:  $XY \parallel X'Y'$

Proof - we know that

$$\angle OPX = 90^\circ \rightarrow (1) \quad (\text{angle at contact point is } 90^\circ)$$

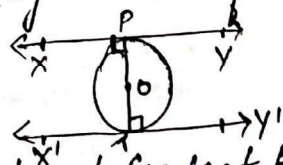
$$\text{and } \angle OTY' = 90^\circ \rightarrow (2) \quad ( \quad " \quad " \quad " \quad " \quad )$$

from eq(1) and (2)

$$\therefore \angle OPX = \angle OTY' \quad (\text{alternate angles})$$

$$\therefore XY \parallel X'Y' \quad (\text{alternate angles are equal})$$

$\hookrightarrow$  Hence proved.





(7)

Ans 24. Angle made by minute hand in 1 minute =  $6^\circ$   
 Angle made by minute hand in 25 minute =  $25 \times 6^\circ$   
 $= 150^\circ$

$$\begin{aligned} \text{Area swept} &= \frac{\theta}{360^\circ} \pi r^2 \\ &= \frac{150}{360} \times \frac{22}{7} \times 14^2 = \frac{770}{3} \text{ sq. cm.} \end{aligned}$$

OR

24.

Let radius of smaller circle be  $r$

A/q

$$\pi (r+3)^2 = 154$$

$$\frac{22}{7} (r+3)^2 = 154$$

$$\frac{22}{7} (r+3)^2 = \frac{154 \times 7}{22} \Rightarrow r+3 = 7$$

$$r = 4$$

$$R = 4+3 = 7$$

Now Area of shaded part

$$\begin{aligned} \pi (R^2 - r^2) &= \pi (R+r)(R-r) \\ &= \frac{22}{7} (7+4)(7-4) = \frac{22 \times 11 \times 3}{7} = \frac{726}{7} \text{ cm}^2 \end{aligned}$$

Ans. 25.

$$3 \sin^2 \alpha + 7 \cos^2 \alpha = 4$$

$$3 \sin^2 \alpha + 7 (1 - \sin^2 \alpha) = 4$$

$$3 \sin^2 \alpha + 7 - 7 \sin^2 \alpha = 4 \Rightarrow \tan \alpha = \tan 60^\circ = \sqrt{3}$$

$$+4 \sin^2 \alpha = +3$$

$$\sin^2 \alpha = 3/4$$

$$\sin \alpha = \frac{\sqrt{3}}{2} \Rightarrow \alpha = 60^\circ$$

OR

$$x = a \sin \alpha \quad y = a \cos \alpha$$

$$\begin{aligned} x^2 + y^2 &= a^2 \sin^2 \alpha + a^2 \cos^2 \alpha \\ &= a^2 (\sin^2 \alpha + \cos^2 \alpha) = a^2 \times 1 = a^2 \end{aligned}$$



(5)

Section C

Ans 26.

Let  $\sqrt{2}$  is rational

$$\Rightarrow \sqrt{2} = p/q \quad (p \text{ \& } q \text{ are co-prime \& } q \neq 0)$$

Squaring both side.

$$2 = \frac{p^2}{q^2} \Rightarrow 2q^2 = p^2 \quad \text{--- (1)}$$

$$\Rightarrow 2 \text{ divides } p^2$$

$$\Rightarrow 2 \text{ divides } p$$

$$\text{Let } p = 2k$$

keeping this in (1)

$$2q^2 = (2k)^2$$

$$\Rightarrow 2q^2 = 4k^2 \Rightarrow 2k^2 = q^2$$

$$\Rightarrow 2 \text{ divides } q^2$$

$$\Rightarrow 2 \text{ divides } q$$

It means  $p$  &  $q$  has common factor 2  
which is against our assumption.

that  $p$  &  $q$  are co-prime.

Hence  $\sqrt{2}$  is irrational.

Ans 27.

$$A+B = -b/a = -(-5)/3 = 5/3 \quad A \cdot B = \frac{c}{a} = \frac{2}{3}$$

Now

$$A^2+B^2 = (A+B)^2 - 2AB = \left(\frac{5}{3}\right)^2 - 2 \times \frac{2}{3} = \frac{25}{9} - \frac{4}{3}$$

$$= \frac{13}{9}$$

Ans. 28.

Let digit at unit place be  $x$ & the digit at ten's place be  $y$ .

$$\text{Number} = 10y + x$$

I case

$$x+y=9 \quad \text{--- (1)}$$

Adding (1) &amp; (2)

$$2x = 10 \quad y = 4$$

$$x = 5$$

II case

$$10x+y = 10y+x+9$$

$$9x-9y=9$$

$$x-y=1 \quad \text{--- (2)}$$

$$\text{Number} = 10 \times 4 + 5 = 45$$

OR

Let the cost of 1 bag = ₹x  
& the cost of 1 pen = ₹y

At I case

$$3x + 4y = 257 \quad (1)$$

$$4x + 3y = 324 \quad (2)$$

Adding (1) & (2)

$$7x + 7y = 581$$

$$\Rightarrow x + y = 83 \quad (3)$$

subtracting (1) from (2)

$$x - y = 67 \quad (4)$$

Adding (3) & (4)

$$2x = 150 \quad y = ₹8$$

$$x = ₹75$$

Now cost of 1 bag and 10 pens

$$75 \times 1 + 8 \times 10 = 75 + 80 = ₹155$$

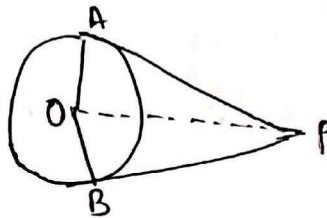
Ans-29. L.H.S. 
$$\sqrt{\frac{1 - \sin \theta}{1 + \sin \theta} \times \frac{1 + \sin \theta}{1 - \sin \theta}} = \sqrt{\frac{(1 - \sin \theta)^2}{1 - \sin^2 \theta}}$$

$$= \sqrt{\frac{(1 - \sin \theta)^2}{\cos^2 \theta}} = \frac{1 - \sin \theta}{\cos \theta} = \frac{1}{\cos \theta} - \frac{\sin \theta}{\cos \theta}$$
$$= \sec \theta - \tan \theta$$

L.H.S. = R.H.S.



Ans. 30.



Given: PA & PB are tangent from same external point

To Prove:  $PA = PB$

Const. Join OA, OB & OP

Proof:  $OA \perp AP$  (radius is  $\perp$  to the point of contact)  
 $OB \perp BP$

In rt  $\triangle OAP$  &  $\triangle OBP$

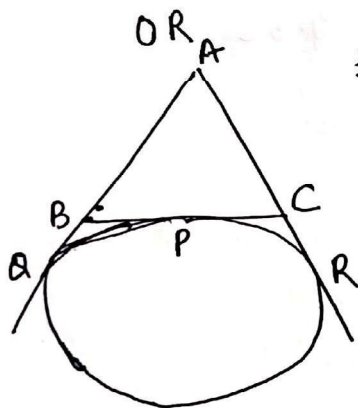
$OA = OB$  (radius)

$OP = OP$  (common)

$\angle OAP = \angle OBP = 90^\circ$

$\triangle OAP \cong \triangle OBP$  (RHS)

$\Rightarrow AP = PB$  (CPCT)



Proof:-  $AQ = AR$  } length of tangent from external point  
 $BQ = BR$   
 $CQ = CR$

Perimeter of  $\triangle ABC = AB + BC + CA$

$= AB + (BQ + CR) + CA$

$= AB + BQ + CR + CA$

$= AQ + AR$

$= AQ + AQ = 2AQ$

$AQ = \frac{1}{2} (\text{Perimeter of } \triangle ABC)$

Ans. 31. Total no. of cases =  $6 \times 6 = 36$ .

(i) Sum of numbers obtained = 6

favourable cases: (1,5) (5,1) (2,4) (4,2) (3,3)

$P(E) = \frac{\text{No. of fav. cases}}{\text{Total no. cases.}} \quad \left| \quad P(\text{sum of no. obtained 6}) = \frac{5}{36}$

(7)

(ii) fav. cases obtained more than 6

(1,6) (6,1) (2,5) (5,2) (6,2) (3,4) (4,3) (3,5) (5,3)

(3,6) (6,3) (4,4) (4,5) (4,6) (6,4) (5,5) (5,6) (6,5) (6,6)

No. of cases = 21 (5,4)

$$P(\text{sum. of no. more than 6}) = \frac{21}{36} = \frac{7}{12}$$

(iii) cases for sum less than 6

(1,1) (1,2) (1,3) (1,4) (2,1) (3,1) (4,1)

(2,2) (2,3) (3,2)

No. of cases = 10

$$P(\text{sum obtained less than 6}) = \frac{10}{36} = \frac{5}{18}$$

Section D.

32. Refer to Page 11 (Umang Test Series) Q. 33

In the given fig

$$\frac{AD}{DB} = \frac{AE}{EC} \quad (\text{BPT})$$

$$\frac{1.5}{3} = \frac{1}{EC} \Rightarrow EC = 2 \text{ cm.}$$

$$33. \text{ Let } \frac{x-2}{x+2} = t$$

$$t^2 + 6 = 5t$$

$$t^2 - 5t + 6 = 0$$

$$t^2 - 3t - 2t + 6 = 0$$

$$t(t-3) - 2(t-3) = 0$$

$$(t-3)(t-2) = 0$$

$$t = 3 \quad t = 2$$

Now

$$\frac{x-2}{x+2} = 3$$

$$x-2 = 3x+6$$

$$-2x = 8$$

$$x = -4$$

Also

$$\frac{x-2}{x+2} = 2$$

$$x-2 = 2x+4$$

$$-x = 6$$

$$x = -6$$



OR

Ans 33

let larger pipe take  $x$  hour to fill the pool  
then smaller pipe will take  $(x+10)$  hrs

Now A/q to case

$$\frac{4}{x} + \frac{9}{x+10} = \frac{1}{2}$$

$$\frac{4x+40+9x}{x(x+10)} = \frac{1}{2} \Rightarrow 26x+80 = x^2+10x$$

$$\Rightarrow x^2-16x-80=0$$

$$x^2-20x+4x-80=0$$

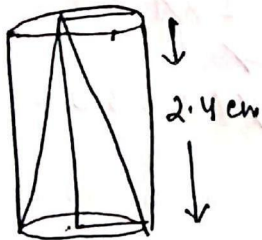
$$x(x-20)+4(x-20)=0$$

$$(x-20)(x+4)=0$$

$$x=20 \quad x \neq -4$$

larger pipe takes 20 hour & smaller pipe takes 30 hours.

Ans 34



$$\text{diameter} = 1.4 \text{ cm}$$

$$h = 2.4 \text{ cm}$$

$$\text{radius} = \frac{1.4}{2} = 0.7 \text{ cm} = \frac{7}{10}$$

$$\text{slant height } (l) = \sqrt{r^2 + h^2}$$

$$= \sqrt{(0.7)^2 + (2.4)^2} = \sqrt{6.25}$$

$$= 2.5 \text{ cm}$$

T.S.A of remaining solid

= CSA of cyl. part + CSA of conical part  
+ Area of cyl. base.

$$= 2\pi rh + \pi rl + \pi r^2$$

$$= \pi r(2h+l+r) = \frac{22}{7} \times \frac{7}{10} \{2 \times 2.4 + 2.5 + 0.7\}$$

$$= 17.60 \text{ cm}^2$$

Now volume of the remaining solid

= volume of cylinder - volume of cone

$$= \pi r^2 h - \frac{1}{3} \pi r^2 h$$

$$= \pi r^2 h \left\{ 1 - \frac{1}{3} \right\} = \frac{2}{3} \pi r^2 h$$

$$= \frac{2}{3} \times \frac{22}{7} \times \frac{22}{10} \times \frac{7}{10} \times \frac{24}{10} = 2.464 \text{ cm}^3$$

OR

$$r+h = 37 \text{ m}$$

$$\text{TSA of cylinder} = 1628 \text{ sq. m}$$

$$2\pi r(r+h) = 1628 \text{ m}^2$$

$$2\pi r \times 37 = 1628 \text{ m}^2$$

$$r = \frac{1628 \times 7}{2 \times 22 \times 37} = 7 \text{ m} \quad h = 30 \text{ m}$$

$$\text{Area of base} = \pi r^2 = \frac{22}{7} \times 7 \times 7 = 154 \text{ m}^2$$

$$\text{Volume} = \pi r^2 h = \frac{22}{7} \times 7 \times 7 \times 30 = 4620 \text{ m}^3$$

Ans. 35. First converting into continuous interval

C.I	F	C.F
-05-9.5	5	5
9.5-19.5	7	12
19.5-29.5	20	32
29.5-39.5	15	47
39.5-49.5	10	57
49.5-59.5	5	62

$$N = \sum f_i = 62$$

$$N/2 = \frac{62}{2} = 31$$

Median class 19.5-29.5

$$\text{Median} = l + \left\{ \frac{N/2 - cf}{f} \right\} \times h$$

$$= 19.5 + \left\{ \frac{31 - 12}{20} \right\} \times 10$$

$$= 19.5 + \frac{19}{2} \times 1$$

$$= 19.5 + 9.5 = 29$$



(12)

## Case study I

- (i) Taking C as origin, the co-ordinates of P are  $(-12, -2)$
- (ii) Taking D as origin, the co-ordinates of Q are  $(-13, 2)$
- (iii)  $P(4, 6)$   $R(6, 5)$   $Q(3, 2)$

$$D = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$PQ = \sqrt{(4-6)^2 + (6-5)^2} = \sqrt{5} \text{ units}$$

$$RQ = \sqrt{(6-3)^2 + (5-2)^2} = \sqrt{18} \text{ units}$$

$$QP = \sqrt{(3-4)^2 + (2-6)^2} = \sqrt{17} \text{ units}$$

$$PQ \neq RQ \neq QP$$

Hence  $\triangle PQR$  is scalene.

Ans 37. Here AP will be 20, 19, 18, ...

$$a = 20 \quad d = -1$$

$$S_n = 200$$

$$\frac{n}{2} [2a + (n-1)d] = 200$$

$$\frac{n}{2} [2 \times 20 + (n-1)(-1)] = 200$$

$$\frac{n}{2} [40 - n + 1] = 200$$

$$\Rightarrow n^2 - 41n + 400 = 0$$

$$n^2 - 16n - 25n + 400 = 0$$

$$n(n-16) - 25(n-16) = 0$$

$$n = 16 \quad n = 25$$

$$a_{25} = a + 24d = 20 + 24(-1)$$

$$= 20 - 24 = -4 \text{ (Not possible)}$$

$$n = 16$$

- (i) No. of rows 16  
middle rows  $8^{\text{th}}$  &  $9^{\text{th}}$

(11)

$$a_8 = a + 7d = 20 + 7(-1) = 13$$

$$a_9 = a + 8d = 20 + 8(-1) = 12$$

(ii) last row has

$$a_{16} = a + 15d = 20 + 15(-1) = 20 - 15 = 5$$

Now logs can be put

$$4 + 3 + 2 + 1 = 10 \text{ logs.}$$

(iii) 20 logs can be put into 16 rows.  
OR.

Top row has 5 logs.

38. (i) In  $\triangle ACB$

$$\frac{AC}{AB} = \sin 60^\circ$$

$$\frac{30}{AB} = \frac{\sqrt{3}}{2} \Rightarrow AB = \frac{60}{\sqrt{3}} = 20\sqrt{3} \text{ m}$$

(ii) In  $\triangle ACD$

$$\frac{AC}{CD} = \tan 45^\circ$$

$$\frac{30}{CD} = 1 \Rightarrow CD = 30 \text{ m}$$

(iii) In  $\triangle ACE$

$$\frac{AC}{CE} = \tan 30^\circ$$

$$\frac{30}{CE} = \frac{1}{\sqrt{3}} \Rightarrow CE = 30\sqrt{3} \text{ m}$$

$$DE = CE - CD = 30\sqrt{3} - 30 = 30(\sqrt{3} - 1) \text{ m}$$

OR

$$BD = BC + CD = (10\sqrt{3} + 30) \text{ m.}$$

$$\frac{AC}{BC} = \tan 60^\circ$$

$$\frac{30}{BC} = \sqrt{3} \Rightarrow BC = \frac{30}{\sqrt{3}} = 10\sqrt{3} \text{ m}$$



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Section A

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By O.P. Gupta, Sachin Pandey, Vishal Minocha

1. (b)

2. (c)

3. (b)

4. (a)

5. (c)

6. (b)

7. (c)

8. (c)

9. (d)

10. (b)

11. (b)

12. (c)

13. (c)

14. (d)

15. (c)

16. (c)

17. (d)

18. (c)

19. (d)

20. (b)

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## Section B

21.  $2x - 5y = 7$

$4x + Ky = 21$

For no solution,

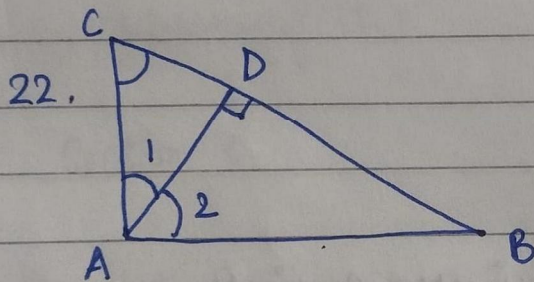
$$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$

I  $\frac{a_1}{a_2} = \frac{b_1}{b_2}$

$$\frac{2}{4} = \frac{-5}{K}$$

$$2K = -20$$

$$K = -10$$



$$\angle 1 + \angle C = 90^\circ$$

$$\angle 1 + \angle 2 = 90^\circ$$

$$\therefore \cancel{\angle 1} + \angle C = \cancel{\angle 1} + \angle 2$$

$$\angle C = \angle 2$$

In  $\triangle CDA$  and  $\triangle ADB$ ,

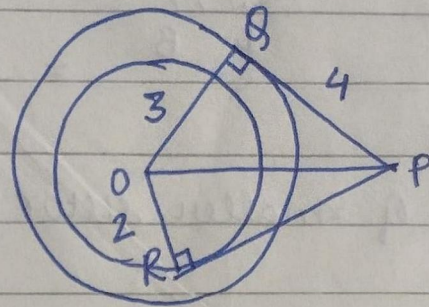
$$\angle D = \angle D (90^\circ)$$

$$\angle A = \angle A (\text{common})$$

$$\therefore \triangle CDA \sim \triangle ADB (\text{by AA})$$

$$\rightarrow \underline{\triangle DBA \sim \triangle PCA}$$

23.



$$\angle OQP = 90^\circ (\text{radius} \perp \text{tangent})$$

$$\angle ORP = 90^\circ (\text{radius} \perp \text{tangent})$$

$$\therefore \text{In } \triangle OQP, OQ^2 + QP^2 = OP^2$$

$$3^2 + 4^2 = OP^2$$

$$9 + 16 = OP^2$$

$$25 = OP^2$$

$$OP = 5 \text{ cm}$$

$$\text{In } \triangle ORP, OR^2 + PR^2 = OP^2$$

$$2^2 + PR^2 = 5^2$$

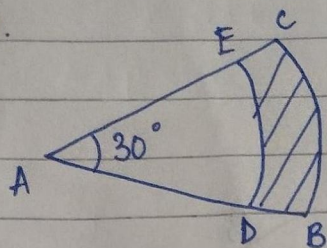
$$4 + PR^2 = 25$$

$$PR^2 = 21$$

$$PR = \underline{\sqrt{21} \text{ cm}}$$



24.



$$\begin{aligned}
 \text{Area of bigger sector} &= \frac{\theta}{360} \times \pi r^2 \\
 &= \frac{30}{360} \times \frac{22}{7} \times 14 \times 14 \\
 &= \frac{11 \times 14}{3} = \frac{154}{3} \text{ cm}^2
 \end{aligned}$$

$$\text{Area of smaller sector} = \frac{\theta}{360} \times \pi r^2$$

$$= \frac{30}{360} \times \frac{22}{7} \times 10.5 \times 10.5 = \frac{11 \times 21}{8} = \frac{231}{8}$$

$$\begin{aligned}
 \text{Area of shaded region} &= \text{Area of bigger sector} - \text{area of small sec.} \\
 &= \frac{154}{3} - \frac{231}{8} = \frac{1232 - 693}{24} = \frac{539}{24} \text{ cm}^2
 \end{aligned}$$

OR. Area of circle =  $616 \text{ cm}^2$

$$\pi R^2 = 616$$

$$R^2 = \frac{616 \times 7}{22} = 28 \times 7$$

$$R = \sqrt{28 \times 7} = 14$$

Length of an arc of each part =  $\frac{\text{perimeter of circle}}{8}$

$$\frac{2\pi R}{8} = \frac{2 \times 22 \times 14}{7 \times 8} = 11 \text{ m}$$

$$\begin{aligned}
 \text{Perimeter of each sector} &= 2R + \text{length of an arc} \\
 &= 28 + 11 = 39 \text{ m}
 \end{aligned}$$

25.  $3 \sin^2 \theta + 7 \cos^2 \theta = 4$

$$3 \sin^2 \theta + 3 \cos^2 \theta + 4 \cos^2 \theta = 4$$

$$3(1) + 4 \cos^2 \theta = 4$$

$$4 \cos^2 \theta = 1$$

$$\cos^2 \theta = \frac{1}{4}$$

$$\cos \theta = \frac{1}{2}$$

$$\cos \theta = \cos 60^\circ$$

$$\theta = 60^\circ$$

$$\tan \theta = ?$$

$$\tan 60^\circ = \sqrt{3}$$

$$\therefore \tan \theta = \sqrt{3}$$



25. DR  $\sin(A+B) = \sin A \cos B + \cos A \sin B$

Let  $A = 45^\circ$ ,  $B = 30^\circ$

$$\sin(45+30) = \sin 75^\circ$$

$$\sin 45^\circ + \cos 30^\circ + \cos 45^\circ \sin 30^\circ$$

$$\frac{1}{\sqrt{2}} \times \frac{\sqrt{3}}{2} + \frac{1}{\sqrt{2}} \times \frac{1}{2}$$

$$\frac{\sqrt{3}}{2\sqrt{2}} + \frac{1}{2\sqrt{2}} = \frac{\sqrt{3}+1}{2\sqrt{2}}$$

$$\frac{\sqrt{3}+1}{2\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}} = \frac{\sqrt{6}+\sqrt{2}}{4}$$

### Section C

26. Let  $5+2\sqrt{3}$  be a rational number.  $5+2\sqrt{3} = \frac{p}{q}$   
Where  $\star q$  &  $p$  are int.  $\star p$  &  $q$  are coprime  $\star q \neq 0$

$$5+2\sqrt{3} = \frac{p}{q}$$

$$2\sqrt{3} = \frac{p}{q} - 5$$

$$\sqrt{3} = \frac{p}{2q} - 5$$

$$\text{LHS} \neq \text{RHS}$$

$\therefore$  Our assumption is wrong

We have a contradiction

Hence,  $5+2\sqrt{3}$  is not rational.

$\Rightarrow 5+2\sqrt{3}$  is irrational.



27.  $3x^2 + 2x + k$

$$x + \beta = \frac{-b}{a} = \frac{-(-2)}{3} = \frac{2}{3}$$

$$x\beta = \frac{c}{a} = \frac{k}{3}$$

$$x^2 + \beta^2 = 6$$

$$(x + \beta)^2 - 2x\beta = 6$$

$$\left(\frac{2}{3}\right)^2 - 2\left(\frac{k}{3}\right) = 6$$

$$\frac{4}{9} - \frac{2k}{3} = 6$$

$$\frac{4 - 6k}{9} = 6$$

$$4 - 6k = 54$$

$$-6k = 50$$

$$k = \frac{-50}{6}$$

$$k = -\frac{25}{3}$$

28. Let units digit be  $x$

Let tens digit be  $y$

$\therefore$  Number =  $10y + x$

Given,  $10y + x + 10x + y = 110$

$$11x + 11y = 110$$

$$x + y = 10 \quad \text{--- (1)}$$

$$x - y = 6 \quad \text{--- (2)}$$

$$x + y = 10$$

$$x - y = 6$$

$$2x = 16$$

$$x = 8$$

Putting value of  $x$  in (1)

$$x + y = 10$$

$$8 + y = 10$$

$$y = 2$$

$$\text{No} = 10x + y = 10(8) + 2$$

$$= 80 + 2 = 82$$

$$\text{Rev. no} = 10y + x$$

$$= 10(2) + 8 = 20 + 8 = 28$$

$\therefore$  Nos = 82, 28



28. OR let numerator be  $n$

let denominator by  $y$

then fraction will be  $\frac{n}{y}$

$$\text{I} \quad \frac{(n+2)}{y} = \frac{1}{2}$$

$$2n+4 = y$$

$$2n - y = -4 \quad \text{--- (i)}$$

$$\text{II} \quad \frac{n}{(y-1)} = \frac{1}{3}$$

$$3n = y-1$$

$$3n - y = -1 \quad \text{--- (ii)}$$

$$2n - y = -4$$

$$3n - y = -1$$

$$\begin{array}{r} - \\ + \end{array}$$

$$-n = -3$$

$$n = 3$$

$$2n - y = -4$$

$$2(3) - y = -4$$

$$6 - y = -4$$

$$-y = -10$$

$$y = 10$$

$$\text{fraction} = \frac{n}{y} = \frac{3}{10}$$

$$29. \quad \tan^2 \theta - \sin^2 \theta = \tan^2 \theta \cdot \sin^2 \theta$$

$$\text{LHS: } \tan^2 \theta - \sin^2 \theta$$

$$= \frac{\sin^2 \theta}{\cos^2 \theta} - \sin^2 \theta$$

$$= \frac{\sin^2 \theta (1 - \cos^2 \theta)}{\cos^2 \theta}$$

$$= \frac{\sin^2 \theta \times \sin^2 \theta}{\cos^2 \theta}$$

$$= \sin^2 \theta \times \tan^2 \theta$$

$$= \text{RHS}$$

Hence, Proved.



30. Given: Circle with centre O. Tangents PQ and PR.

To prove:  $PQ = PR$

Const: Join OQ, OR, PO

Proof: In  $\triangle POR$  and  $\triangle POQ$

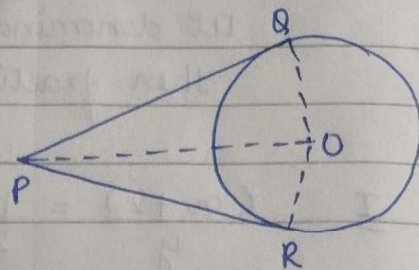
$$PO = PO \text{ (common)}$$

$$OQ = OR \text{ (radii)}$$

$$\angle ORP = \angle OQP = 90^\circ \text{ (radius } \perp \text{ tangent)}$$

$$\triangle POR \cong \triangle POQ \text{ (by RHS)}$$

$$\therefore PR = PQ \text{ (cpct)}$$



OR. Given: Circle with centre O.

To prove:  $XA + AR = XB + BR$

Proof:  $XP = XQ$  (tangents from ext. pt are eq.)

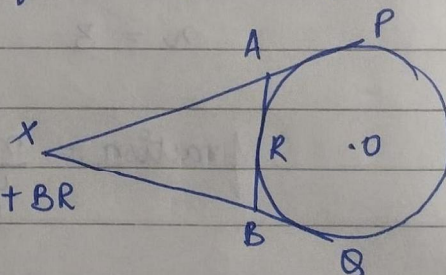
$$AP = AR, \quad BQ = BR$$

$$XP = XA + AP \text{ --- (1)}$$

$$XQ = XB + BQ \text{ --- (2)}$$

$$\Rightarrow XP = XA + AR, \quad XQ = XB + BR$$

$$\therefore XA + AR = XB + BR$$



31.  $P(\text{Same numbers}) = (1,1)(2,2)(3,3)(4,4)(5,5)(6,6)$

No. of favourable outcomes = 6, Total = 36

$$(i) P(\text{same nos.}) = \frac{\text{No. of favourable outcomes}}{\text{Total no. of outcomes}} = \frac{6}{36} = \frac{1}{6}$$

(ii)  $P(\text{product } 12) = (2,6)(3,4)(4,3)(6,2)$

No. of favourable outcomes = 4

$$P(\text{product as } 12) = \frac{\text{No. of favourable outcomes}}{\text{Total no. of outcomes}} = \frac{4}{36} = \frac{1}{9}$$

(iii)  $P(\text{diff. as } 1) = (1,2)(2,1)(3,4)(4,3)(4,5)(5,4)$   
 $(3,2)(2,3)(5,6)(6,5)$

No. of favourable outcomes = 10

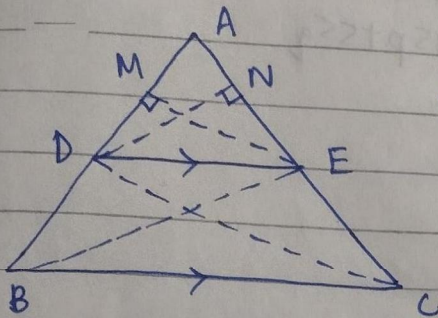
$$P(\text{diff. as } 1) = \frac{10}{36} = \frac{5}{18}$$



## Section D

### 32. Basic Proportionality Theorem (BPT)

STATEMENT: If a line is drawn parallel to one side of a triangle then it divides the other two sides in the same ratio.



Given:  $\triangle ABC$ ,  $DE \parallel BC$

To prove:  $\frac{AD}{DB} = \frac{AE}{EC}$

Const:  $EM \perp AD$ ,  $DN \perp AE$

Join B to E, C to D

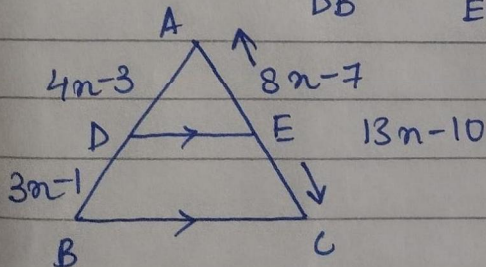
$$\text{Proof: } \frac{\text{ar}(\triangle ADE)}{\text{ar}(\triangle BDE)} = \frac{\frac{1}{2} \times AD \times EM}{\frac{1}{2} \times BD \times EM} = \frac{AD}{BD} \quad \text{--- (1)}$$

$$\frac{\text{ar}(\triangle ADE)}{\text{ar}(\triangle CDE)} = \frac{\frac{1}{2} \times AE \times DN}{\frac{1}{2} \times CE \times DN} = \frac{AE}{CE} \quad \text{--- (2)}$$

$$\text{ar}(\triangle BDE) = \text{ar}(\triangle CDE) \quad [\text{Triangles on same parallels}] \quad \text{--- (3)}$$

$\therefore$  From (1), (2), and (3)

$$\frac{AD}{DB} = \frac{AE}{EC}$$



$$EC = AC - AE$$

$$= 13n - 10 - (8n - 7)$$

$$= 13n - 10 - 8n + 7 = 5n - 3$$

$$\frac{4n-3}{3n-1} = \frac{8n-7}{5n-3} \quad \left[ \frac{AD}{DB} = \frac{AE}{EC} \right]$$

$$(4n-3)(5n-3) = (3n-1)(8n-7)$$

$$20n - 12n - 15n + 9 = 24n - 21n - 8n + 7$$

$$-7n + 9 = -5n + 7$$

$$-2n = -2$$

$$\underline{n = 1}$$



$$33. \quad n^2 - 2(a^2 + b^2)n + (a^2 - b^2)^2 = 0$$

$$n^2 - 2(a^2 + b^2)n + [(a+b)(a-b)]^2 = 0$$

$$n^2 - 2a^2 - 2b^2n + (a+b)^2(a-b)^2 = 0$$

$$n^2 - (a+b)^2n - (a-b)^2n + (a+b)^2 - (a-b)^2 = 0$$

$$n[n - (a+b)^2] - [a-b]^2[n + (a+b)^2] = 0$$

$$[n - (a+b)^2][n - (a-b)^2] = 0$$

$$\Rightarrow n = (a+b)^2 \quad \text{or} \quad n = (a-b)^2$$

OR. Let Rohan's present age be  $n$  years

His mother's age =  $(n+26)$  yrs

Rohan's age after 3 years =  $(n+3)$  yrs

Mother's age after 3 years =  $(n+26+3) = (n+29)$  yrs

Product of ages 3 yrs later =  $(n+3)(n+29) = 360$

$$\Rightarrow n^2 + 29n + 3n + 87 = 360$$

$$\Rightarrow n^2 + 32n - 273 = 0$$

$$n^2 + 39n - 7n - 273 = 0$$

$$n(n+39) - 7(n+39) = 0$$

$$(n+39)(n-7)$$

$$n = -39 \text{ (rejected)} \quad n = 7$$

$\therefore$  Rohan's age =  $n = 7$  years

His mother's age =  $n+26 = 7+26 = 33$  years



Q34 DR

$$V = 41 \frac{19}{21} \text{ dm}^3$$

$$V_{\text{cyl}} + V_{\text{hemi}} = \frac{880}{21}$$

$$\pi r^2 h + \frac{2}{3} \pi r^3 = \frac{880}{21}$$

$$\frac{22}{7} \times r^3 \left( 1 + \frac{2}{3} \right) = \frac{880}{21}$$

$$\frac{22}{7} \times r^3 \times \frac{5}{3} = \frac{880}{21}$$

$$r^3 = \frac{880}{22 \times 5}$$

$$r^3 = 8$$

$$r = 2$$

$$h = 2r = 4 \text{ m (ht. of the building)}$$

(34)

$$\text{Outer CSA} - \text{Inner CSA} = 44$$

$$2\pi R h - 2\pi r h = 44$$

$$2 \times \frac{22}{7} \times 14 (R - r) = 44$$

$$R - r = \frac{44 \times 7}{2 \times 22 \times 14} = \frac{1}{2} \quad \text{--- (i)}$$

$$R - r = \frac{1}{2} \quad \text{--- (i)}$$

$$\text{Outer V} - \text{inner V} = 99$$

$$\pi R^2 h - \pi r^2 h = 99$$

$$\frac{22}{7} \times 14 (R^2 - r^2) = 99$$

$$(R + r)(R - r) = \frac{99}{4} \quad \text{--- (ii)}$$

$$(R + r) \left( \frac{1}{2} \right) = \frac{9}{4} \quad \text{--- (ii)}$$

$$R + r = \frac{9}{2} \quad \text{--- (ii)}$$

$$R - r = 0.5$$

$$R + r = 4.5$$

$$2R = 5$$

$$R = \frac{5}{2} = 2.5 \text{ cm}$$

$$r = 4.5 - 2.5 = 2 \text{ cm}$$



35. Class (CI)	freq	$n_i$	$f_i n_i$	
0-10	5	5	25	$595 + 45p + 55q = \sum f_i n_i$
10-20	7	15	105	
20-30	13	25	325	
30-40	4	35	140	
40-50	$p$	45	$45p$	
50-60	$q$	55	$55q$	
	<u>50</u>		<u><math>595 + 45p + 55q</math></u>	

$$29 + p + q = 50$$

$$p + q = 21$$

$$q = 21 - p$$

$$\bar{x} = \frac{\sum f_i n_i}{\sum f_i}$$

$$32.8 = \frac{595 + 45p + 55q}{50} = \frac{8(119 + 9p + 11q)}{50 \cdot 10}$$

$$328 = 119 + 9p + 11q$$

$$209 = 9p + 11(21 - p)$$

$$209 = 9p + 231 - 11p$$

$$209 - 231 = 9p - 11p$$

$$-22 = -2p$$

$$11 = p$$

$$q = 21 - 11 = 10$$

$$\underline{p = 11, q = 10}$$

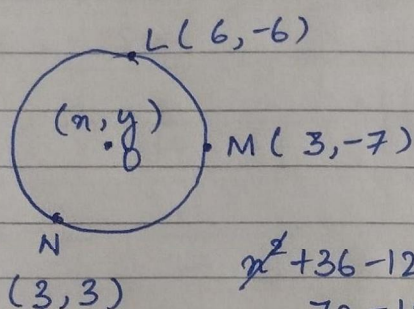


# Section E

36.  $L(6, -6)$   $M(3, -7)$   $N(3, 3)$

$$\begin{aligned} \text{(i)} \quad LM &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= \sqrt{(3 - 6)^2 + (-7 + 6)^2} \\ &= \sqrt{(3)^2 + (-1)^2} \\ &= \sqrt{9 + 1} = \sqrt{10} \text{ units} \end{aligned}$$

ii)



$$OL = OM$$

$$OL^2 = OM^2$$

$$\begin{aligned} (n - 6)^2 + (y + 6)^2 &= (n - 3)^2 + (y + 7)^2 \\ n^2 + 36 - 12n + y^2 + 36 + 12y &= n^2 + 9 - 6n + y^2 + 49 + 14y \\ 72 - 12n + 12y &= 58 - 6n + 14y \end{aligned}$$

$$14 - 6n - 2y = 0$$

$$-3n - y = -7 \Rightarrow 3n + y = 7$$

$\begin{aligned} OM^2 &= ON^2 \\ (n - 3)^2 + (y + 7)^2 &= (n - 3)^2 + (y - 3)^2 \\ y^2 + 49 + 14y &= y^2 + 9 - 6y \\ 20y &= -40 \\ y &= -2 \end{aligned}$	$\begin{aligned} 3n + y &= 7 \\ 3n - 2 &= 7 \\ 3n &= 9 \\ n &= 3 \end{aligned}$
---	---

$\therefore$  Coordinates of the centre  $= (n, y) = (3, -2)$

$$\begin{aligned} \text{(ii)} \quad ON &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= \sqrt{(3 - 3)^2 + (3 + 2)^2} \\ &= \sqrt{25} = 5 \text{ units (radius of circle)} \end{aligned}$$

iii) OR  $\left( \frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3} \right)$  centroid of  $\triangle LMN$

$$= \left( \frac{6 + 3 + 3}{3}, \frac{-6 - 7 + 3}{3} \right) = \left( \frac{12}{3}, \frac{-10}{3} \right) = \left( 4, -\frac{10}{3} \right)$$



37.  $1, 2, 3, \dots, n-1, n, n+1, \dots, 49$

$$(iii) S_{n-1} = S_{49} - S_n$$

$$S_{n-1} + S_n = S_{49}$$

$$\frac{(n-1)(n-1+1)}{2} + \frac{n(n+1)}{2} = \frac{49 \times 50}{2}$$

$$\frac{n^2 - \cancel{n} + n^2 + \cancel{n}}{2} = \frac{49 \times 50}{2}$$

$$\frac{2n^2}{2} = 49 \times 25$$

$$n^2 = 49 \times 25$$

$$n = \sqrt{49 \times 25}$$

$$n = 7 \times 5 = \underline{35}$$

(i) Sum of all house no. preceding  $n = S_{34}$

$$S_{34} = \frac{34 \times 35}{2} = 595 \quad (S_n \text{ of } n \text{ natural no's} = \frac{n(n+1)}{2})$$

(ii) Total no of houses = 49

$$\text{middle most house} = \frac{n+1}{2} = \frac{49+1}{2} = 25$$

(iii)  $n = 35$

OR AP of multiples of 2 =  $2, 4, 6, 8, \dots, 48$ ,  $n = \frac{48}{2} = 24$

AP of multiples of 3 =  $3, 6, 9, 12, \dots, 48$ ,  $n = \frac{48}{3} = 16$

$$S_{24} = \frac{24}{2} (2+48) = 12(50) = 600$$

$$S_{16} = \frac{16}{2} (3+48) = 8(51) = 408$$

$$S_8 = \frac{8}{2} (6+48) = 4(54) = 216$$

{ AP of multiples of 6 =  $6, 12, \dots, 48$  }

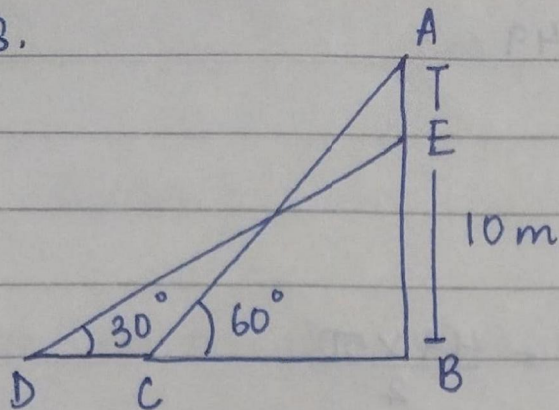
$$S = S_{24} + S_{16} = S_8 \quad \{ \text{because 6 is a common multiple} \}$$

$$S = 600 + 408 - 216$$

$$= 1008 - 216 = 792$$

$\therefore$  Sum of house numbers which are a multiple of 2 or 3 is 792.

38.



AB is Wall = 10m

$$(i) \text{ In } \triangle ABC, \sin 60^\circ = \frac{AB}{AC}$$

$$\frac{\sqrt{3}}{2} = \frac{10}{AC}$$

$$\sqrt{3} AC = 20$$

$$AC = \frac{20}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = \frac{20\sqrt{3}}{3} = \frac{20 \times 1.73}{3} = 11.5 \text{ m}$$

$$(ii) \text{ In } \triangle ABC, \tan 60^\circ = \frac{AB}{BC}$$

$$\sqrt{3} = \frac{10}{BC}$$

$$\sqrt{3} BC = 10$$

$$BC = \frac{10\sqrt{3}}{3} = 5.7 \text{ m}$$



38.

10m

y m

20√3

20/√3

60°

30°

D

x

C

B

10/√3

(ii)  $AB = 10\text{m}$

In  $\triangle ABD$ ,

$$\tan 60 = \frac{10}{BD}$$

$$\sqrt{3} = \frac{10}{BD}$$

$$\frac{BD}{\sqrt{3}} = \frac{10}{\sqrt{3}}$$

Now, In  $\Delta MBC$

$$\cos 30^\circ = \frac{10}{\sqrt{3}} + \frac{\pi}{1}$$

$$\frac{\sqrt{3}}{2} = \frac{10 + \sqrt{3}x}{\sqrt{3}}$$

$$\frac{\sqrt{3}}{2} = \frac{10 + \sqrt{3}n}{2010}$$

$$10\sqrt{3} = 10 + \sqrt{3}n$$

$$\frac{10(\sqrt{3}-1)}{\sqrt{3}} = x$$

$$n = 4.3 \text{ m} \quad \underline{\underline{\text{Ans}}}$$



OR. (iii)

In  $\triangle CBM$ ,

$$\sin 30 = \frac{BM}{CM}$$

$$\frac{1}{2} = \frac{BM}{\frac{10}{\sqrt{3}}}$$

$$\frac{1}{2} = \frac{\sqrt{3} BM}{10}$$

$$10 = \sqrt{3} BM$$

$$\frac{10}{\sqrt{3}} = BM$$

$$AB = AM + BM$$

$$10 = y + \frac{10}{\sqrt{3}}$$

$$10 - \frac{10}{\sqrt{3}} = y$$

$$\frac{10\sqrt{3} - 10}{\sqrt{3}} = y$$

$$\frac{10(\sqrt{3} - 1)}{\sqrt{3}} = y$$

$$\boxed{y = 4.3m} \quad \text{Ans}$$



**SOLUTIONS FOR UTS-19**  
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**O.P. GUPTA**  
**SACHIN PANDEY**  
**VISHAL MINOCHA**

Ans 1 -

$$\begin{array}{r|l} 3 & 255 \\ \hline 5 & 85 \\ \hline 17 & 17 \\ \hline & 1 \end{array}$$

3 is a factor of 255.

$$\begin{array}{r|l} 5 & 255 \\ \hline 51 & 51 \\ \hline & 1 \end{array}$$

5 is a factor of 255.

$$\begin{array}{r|l} 17 & 255 \\ \hline 5 & 15 \\ \hline 3 & 3 \\ \hline & 1 \end{array}$$

17 is a factor of 255.

Hence, 25 is not a factor of 255.

Ans  $\Rightarrow$  b). 25

Ans 2 -

$$\begin{aligned} \text{class mark} &= \frac{\text{upper limit} + \text{lower limit}}{2} \\ &= \frac{19.5 + 29.5}{2} = \frac{49}{2} = 24.5 \end{aligned}$$

Ans  $\Rightarrow$  (c). 24.5

Ans 3 -

Let the radius of bigger circle (R) be 4cm  
and the radius of smaller circle (r) be 2cm.

$$\begin{aligned} \text{Area} &= \text{Area of bigger circle} - \text{Area of smaller circle} \\ &= \pi R^2 - \pi r^2 \\ &= \pi [R^2 - r^2] \\ &= \pi [(4)^2 - (2)^2] \\ &= \pi [16 - 4] \\ &= \pi [12] \\ &= 12\pi \text{ sq. cm} \end{aligned}$$

Ans  $\Rightarrow$  a).  $12\pi$  sq. cm

By O.P. GUPTA, SACHIN PANDEY, VISHAL MINOCHA

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Ans4-

$$\text{Mean} = \frac{\text{Sum of observation}}{\text{Total no. of observation}}$$

$$\Rightarrow \frac{3+5+5+7+7+7+9+9+9+9}{10}$$

$$\Rightarrow \frac{70}{10} = 7$$

Number of favourable cases of 7 = 3

$$P(\text{No. of favourable cases of 7}) = \frac{\text{No. of outcomes}}{\text{Total no. of outcomes}}$$

$$\Rightarrow \frac{3}{10} = 0.3$$

Ans  $\Rightarrow$  b). 0.3

Ans5-

$$4x^2 - 1$$

Zeros of  $4x^2 - 1$

$$\Rightarrow 4x^2 - 1 = 0$$

$$\Rightarrow 4x^2 = 1$$

$$\Rightarrow x^2 = \frac{1}{4}$$

$$\Rightarrow x = \pm \sqrt{\frac{1}{4}}$$

$$\Rightarrow x = \pm \frac{1}{2}$$

Zeros are  $\frac{1}{2}$  and  $-\frac{1}{2}$

Ans  $\Rightarrow$  b).  $\frac{1}{2}$ ,  $-\frac{1}{2}$

Ans6-

Given :  $DE \parallel BC$

$$AB = 5.6 \text{ cm}$$

$$AD = 1.6 \text{ cm}$$

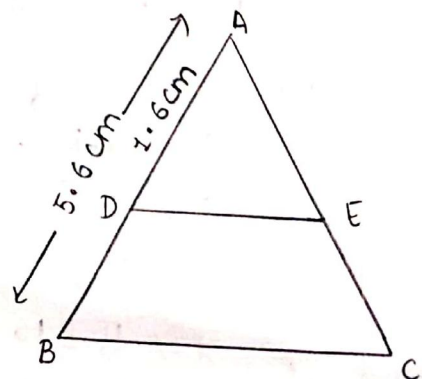
$$\frac{AD}{DB} = \frac{AE}{EC}$$

$$AB - AD = DB$$

$$5.6 - 1.6 = DB$$

$$4.0 = DB$$

$$DB = 4 \text{ cm}$$



$$\frac{AD}{DB} = \frac{AE}{EC}$$

$$\Rightarrow \frac{1.6}{4.0} = \frac{AE}{EC}$$

$$\Rightarrow \frac{2}{5} = \frac{AE}{EC}$$

$$\Rightarrow AE : EC = 2 : 5$$

Ans  $\Rightarrow$  d). 2 : 5

Ans 7-

Given : central angle =  $90^\circ$   
radius = 7cm

$$\begin{aligned} \text{Perimeter of sector} &= 2r + \frac{2\pi r \theta}{360} \\ &= 2 \times 7 + \frac{2 \times \frac{22}{7} \times 7 \times 90}{360} \\ &= 14 + 11 = 25 \end{aligned}$$

Ans  $\Rightarrow$  b). 25cm

Ans 8-

$2x + 3y = 6 \rightarrow$  Equation of pair of dependent linear equations.

Second equation will be  $\Rightarrow 4x + 6y = 12$   
 $\Rightarrow 2x + 3y = 6$

Ans  $\Rightarrow$  c).  $4x + 6y = 12$

Ans 9-

a). tangent

Ans 10-

$$\cos 90 = \frac{1}{\sqrt{2}}$$

$$\cos 90 = \cos 45^\circ$$

$$90 = 45^\circ$$

$$0 = \frac{45}{9}$$

$$0 = 5^\circ$$

$$\begin{aligned} \text{To find: } \tan 60 &= \tan 6 \times 5^\circ \\ &= \tan 30^\circ \\ &= \frac{1}{\sqrt{3}} \end{aligned}$$

Ans  $\Rightarrow$  b).  $\frac{1}{\sqrt{3}}$



Ans 11-

$$\sqrt{25} \times \sqrt{4} = \sqrt{100} = 10$$

$$\text{Ans} \Rightarrow \text{b). } \sqrt{25}, \sqrt{4}$$

Ans 12-

Given: PA & PB (tangents to the circle)

$$\angle OAB = 25^\circ$$

To find:  $\angle APB$

Proof: PA = PB (given)

$\angle 2 = \angle 3$  (Isosceles property)

$$\angle 2 + \angle 4 = 90^\circ$$

(Radius is perpendicular to point of contact)

$$\angle 1 + \angle 2 + \angle 3 = 180^\circ \text{ (Angle sum property)}$$

$$\angle 1 + \angle 2 + \angle 2 = 180^\circ$$

$$\angle 1 + 2\angle 2 = 180^\circ$$

$$\angle 1 + \angle 2 (90^\circ - \angle 4) = 180^\circ$$

$$\angle 1 + 180^\circ - 2\angle 4 = 180^\circ$$

$$\angle 1 - 2\angle 4 = 180^\circ - 180^\circ$$

$$\angle 1 = 2\angle 4$$

$$\angle APB = 2\angle OAB$$

$$\angle APB = 50^\circ$$

$$\text{Ans} \Rightarrow \text{b). } 50^\circ$$

Ans 13-

$$\begin{aligned} \frac{1 + \tan^2 \beta}{1 + \cot^2 \beta} &= \frac{1 + \frac{\sin^2 \beta}{\cos^2 \beta}}{\frac{1 + \cos^2 \beta}{\sin^2 \beta}} = \frac{\frac{\cos^2 \beta + \sin^2 \beta}{\cos^2 \beta}}{\frac{\sin^2 \beta + \cos^2 \beta}{\sin^2 \beta}} \\ &= \frac{1}{\frac{\cos^2 \beta}{\sin^2 \beta}} = \frac{\sin^2 \beta}{\cos^2 \beta} = \tan^2 \beta \end{aligned}$$

$$\text{Ans} \Rightarrow \text{a). } \tan^2 \beta$$

Ans 14-

Perimeter of one triangle be  $(P_1) = 25\text{cm}$

Perimeter of other triangle be  $(P_2) = 15\text{cm}$

Ratio of perimeter of similar triangle is equal to corresponding sides of triangle.

$$\frac{P_1}{P_2} = \frac{a_1}{a_2} \Rightarrow \frac{25}{15} = \frac{a_1}{a_2}$$

$$\frac{a_1}{a_2} = \frac{25}{15}$$

$$\Rightarrow \frac{9}{a_2} = \frac{5}{3}$$

$$\Rightarrow 27 = 5a_2$$

$$\Rightarrow a_2 = 5.4\text{cm}$$

Ans  $\Rightarrow$  b).  $5.4\text{cm}$

Ans 15-

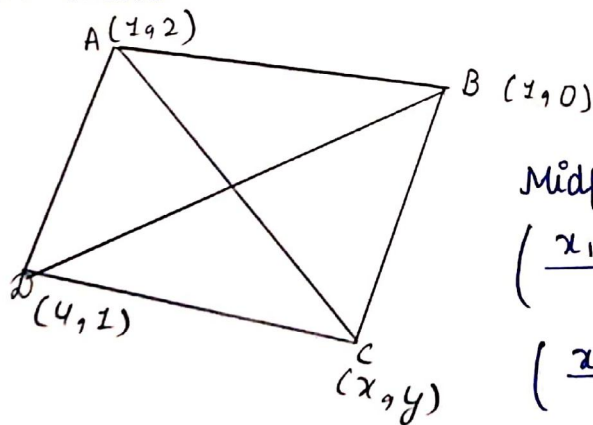
$$\frac{21}{24.5^7} = \frac{21}{1250000} = 0.0000168$$

Ans  $\Rightarrow$  c).  $0.0000168$

Ans 16-

c). Cubic

Ans 17-



Let C coordinates be  $(x, y)$ .

Midpoint of AC = Midpoint of BD

$$\left( \frac{x_1 + x_2}{2} \right) = \left( \frac{y_1 + y_2}{2} \right)$$

$$\left( \frac{x+1}{2}, \frac{y+2}{2} \right) = \left( \frac{4+1}{2}, \frac{1+0}{2} \right)$$

$$\left( \frac{x+1}{2}, \frac{y+2}{2} \right) = \left( \frac{5}{2}, \frac{1}{2} \right)$$

Now,

$$\frac{x+1}{2} = \frac{5}{2}$$

$$x = 5 - 1$$

$$x = 4$$



$$\frac{y+2}{x} = \frac{1}{x}$$

$$y = 1 - 1$$

$$y = -1$$

Ans 18-

$$\sec \theta - \tan \theta = k \text{ (given)}$$

To find:  $\sec \theta + \tan \theta$

$$\sec \theta - \tan \theta = k$$

$$\text{we know, } \sec^2 \theta - \tan^2 \theta = 1$$

$$(\sec \theta - \tan \theta)(\sec \theta + \tan \theta) = 1$$

$$k(\sec \theta + \tan \theta) = 1$$

$$\sec \theta + \tan \theta = \frac{1}{k}$$

$$\text{Ans} \Rightarrow \text{C). } \frac{1}{k}$$

Ans 19-

Ans  $\Rightarrow$  C). A is true but R is false.

Ans 20-

Ans  $\Rightarrow$  a). Both A and R is true and R is the correct explanation of A.

### Section-B

Ans 21-

$$21x + 47y = 110 \text{ — (1)}$$

$$47x + 21y = 162 \text{ — (2)}$$

Adding eq (1) + (2)

$$68x + 68y = 272$$

$$x + y = 4 \text{ — (3)}$$

Subtracting eq (1) - (2)

$$26x - 26y = 52$$

$$x - y = 2 \text{ — (4)}$$

By elimination method eq (3) + (4)

$$2x = 6$$

$$x = 3$$

putting  $x = 3$  in eq (3)

$$x + y = 4$$

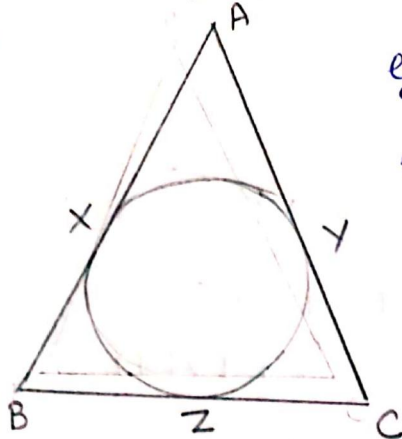
$$3 + y = 4$$

$$y = 4 - 3$$

$$y = 1$$

Hence, the value of  $x$  and  $y$  is 3 and 1.

Ans 22-



Given:  $ABC$  is an isosceles triangle  
 $AB = AC$

To prove:  $BC$  is bisected at a point of contact

Proof:

$$AX = AY$$

$$BX = BZ$$

$$CY = CZ$$

[Tangent from same external points are equal.]

It is given  $ABC$  is an isosceles triangle,

$$\Rightarrow AB - AX = AC - AY$$

$$\Rightarrow BX = CY$$

$$\Rightarrow BZ = CZ$$

Therefore,  $BZ = CZ$ . Hence,  $BC$  is bisected at point of contact.

Ans 23-

Given:  $\angle ACB = 50^\circ$   
 $AOC$  = diameter of circle

To prove:  $\angle BAT$

Proof:  $\angle CBA = 90^\circ$   
 (Angle of semi-circle is right angle)

$$\angle CAB + \angle CBA + \angle ACB = 180^\circ \text{ (Angle sum property)}$$

$$\angle CAB + 90^\circ + 50^\circ = 180^\circ$$

$$\angle CAB + 140^\circ = 180^\circ$$

$$\angle CAB = 40^\circ$$

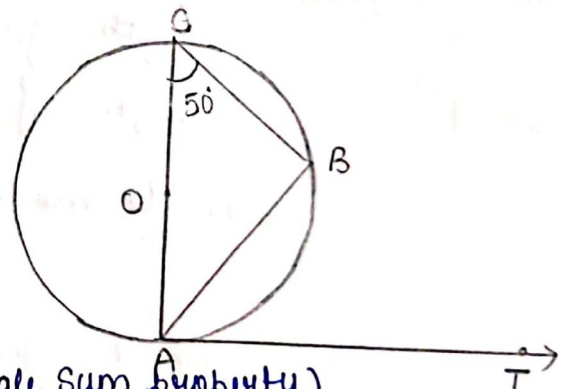
$OA \perp OT$  [Radius is perpendicular to tangent at point of contact]

$$\text{So, } \angle CAB + \angle BAT = 90^\circ$$

$$40^\circ + \angle BAT = 90^\circ$$

$$\angle BAT = 50^\circ$$

Therefore,  $\angle BAT = 50^\circ$ .





Ans 24. (II Part) 'Osh'

Radius of semi-circle = 7cm

$$\begin{aligned}\text{Circumference of semi-circle} &= \pi r + 2r \\ &= \frac{22}{7} \times 7 + 2(7) \\ &= 22 + 14 \\ &= 36\text{cm}\end{aligned}$$

Hence, the perimeter of semicircle is 36cm.

Ans 24 (I part)

length of minute hand( $R$ ) = 14cm

length of hour hand( $r$ ) = 7cm.

Angle made by minute hand in 90 minutes.  
 $= 90 \times 6^\circ = 540^\circ$

Angle made by hour hand in 90 minutes  
 $= \frac{3}{2} \times 30^\circ = 45^\circ$

Distance travelled by minute hand  
 $= \frac{\theta}{360^\circ} \times 2\pi R = \frac{540}{360} \times 2 \times \frac{22}{7} \times 14 = 132\text{cm}$

Distance travelled by hour hand  
 $= \frac{\theta}{360^\circ} \times 2\pi r = \frac{45}{360} \times 2 \times \frac{22}{7} \times 7 = 5.5\text{cm}$

total distance =  $132 + 5.5 = 137.5\text{cm}$ .

Ans. 25(I)  $\sin X = \frac{199}{201}$

$$\Rightarrow (\tan^2 X + \cot^2 X) - (\sec^2 X + \operatorname{cosec}^2 X)$$

$$\Rightarrow \left( \frac{\sin^2 X}{\cos^2 X} + \frac{\cos^2 X}{\sin^2 X} \right) - \left( \frac{1}{\cos^2 X} + \frac{1}{\sin^2 X} \right)$$

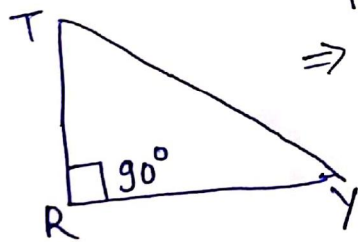
$$\Rightarrow \left( \frac{\sin^4 X + \cos^4 X}{\sin^2 X \cos^2 X} \right) - \left( \frac{\sin^2 X + \cos^2 X}{\sin^2 X \cos^2 X} \right)$$

$$= \left( \frac{(\sin^2 X + \cos^2 X)^2 - 2\sin^2 X \cos^2 X}{\sin^2 X \cos^2 X} \right) - \left( \frac{1}{\sin^2 X \cos^2 X} \right)$$

$$= \frac{1 - 2\sin^2 X \cos^2 X}{\sin^2 X \cos^2 X} - \frac{1}{\sin^2 X \cos^2 X}$$

$$= \frac{\cancel{1} - 2\sin^2 X \cos^2 X - \cancel{1}}{\sin^2 X \cos^2 X} = \frac{-2\sin^2 X \cos^2 X}{\sin^2 X \cos^2 X} = -2$$

OR II



$$\begin{aligned} TR &= RY \\ \Rightarrow \angle T &= 45^\circ \quad \angle Y = 45^\circ \\ \angle R &= 90^\circ \end{aligned}$$

$$\begin{aligned} \text{Now } \cos T + \cos R + \cos Y \\ \cos 45^\circ + \cos 90^\circ + \cos 45^\circ \\ \frac{1}{\sqrt{2}} + 0 + \frac{1}{\sqrt{2}} \\ = \frac{2}{\sqrt{2}} = \sqrt{2} \end{aligned}$$



### Section - C

Ans 26-

Let  $\sqrt{3}$  is irrational.

$$\sqrt{3} = \frac{a}{b}$$

(where  $a$  and  $b$  are co-prime &  
 $b \neq 0$ )

squaring both sides,

$$(\sqrt{3})^2 = \left(\frac{a}{b}\right)^2$$

$$3 = \frac{a^2}{b^2}$$

$$3b^2 = a^2$$

$\therefore 3$  divides  $a^2$

$\therefore 3$  divides  $a$

$$3b^2 = (3k)^2$$

$$3b^2 = 9k^2$$

$$b^2 = 3k^2$$

(where  $k$  is some integer)

$\Rightarrow 3$  divides  $b^2$

$\therefore 3$  divides  $b$

It means  $a$  &  $b$  has 3 as a common factor which is against our assumption that  $a$  &  $b$  are co-prime  
hence  $\sqrt{3}$  is irrational.

Let  $\sqrt{3} - 5 = \frac{a}{b}$  (where  $a$  and  $b$  are co-prime  
 &  $b \neq 0$ )

$$\sqrt{3} = \frac{a}{b} + 5$$

$$\sqrt{3} = \frac{a+5b}{b}$$

Hence,  $\frac{a+5b}{b}$  is rational but  $\sqrt{3}$  is irrational  
 which means our assumption is wrong.

Ans 27-

$$4x^2 - 7x + 3 \quad (a=4, b=-7, c=3)$$

$$\Rightarrow 4x^2 - 4x - 3x + 3$$

$$\Rightarrow 4x(x-1) - 3(x-1)$$

$$\Rightarrow (4x-3)(x-1)$$

$$x = \frac{3}{4}, x = 1$$

Verifying relationship

$$\text{Sum of zeroes} = -\frac{b}{a}$$

$$\alpha + \beta = -\frac{b}{a}$$

$$\frac{3}{4} + 1 = -\frac{(-7)}{4}$$

$$\frac{3+4}{4} = \frac{7}{4}$$

$$\frac{7}{4} = \frac{7}{4}$$

$$\text{Product of zeroes} = \frac{c}{a}$$

$$\alpha\beta = \frac{c}{a}$$

$$\frac{3}{4} \times 1 = \frac{3}{4}$$

$$\frac{3}{4} = \frac{3}{4}$$

Hence verified



Ans 28-

For infinite solution,

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$$

$$2x - 3y = 7$$

$$(a+b)x - (a+b-3)y = 4a+b$$

$$\frac{2}{a+b} = \frac{-3}{-(a+b-3)} = \frac{-7}{-(4a+b)}$$

$$\frac{2}{a+b} = \frac{3}{(a+b-3)} = \frac{7}{(4a+b)}$$

Now,

$$\frac{2}{a+b} = \frac{3}{(a+b-3)}$$

$$2a + 2b - 6 = 3a + 3b$$

$$\Rightarrow -a - b = 6$$

$$\Rightarrow a + b = -6 \text{ --- (1)}$$

$$\frac{2}{a+b} = \frac{7}{4a+b}$$

$$\Rightarrow 8a + 2b = 7a + 7b$$

$$\Rightarrow a - 5b = 0 \text{ --- (2)}$$

By elimination method, both the equation  
 $b = -1$

putting  $b = -1$  in eq (1)

$$a + b = -6$$

$$a - 1 = -6$$

$$a = -5$$

Hence, the value of  $a$  and  $b$  is  $-5$  &  $-1$ .  
'or'

Let the numerator be  $x$

Let the denominator be  $y$ .

A/q 1<sup>st</sup> condition

$$\Rightarrow \frac{x-2}{y} = \frac{1}{3}$$

$$\Rightarrow 3x - 6 = y$$

$$\Rightarrow 3x - y = 6 \quad \text{--- (1)}$$

Ans/q II<sup>nd</sup> condition

$$\frac{x}{y-1} = \frac{1}{2}$$

$$2x = y - 1$$

$$2x - y = -1 \quad \text{--- (2)}$$

By elimination method,

we get,  $x = 7$

putting  $x = 7$  in eq (1)

$$3x - y = 6$$

$$3(7) - y = 6$$

$$21 - y = 6$$

$$-y = 6 - 21$$

$$-y = -15$$

$$y = 15$$

Therefore, fraction is  $\frac{7}{15}$ .

Ans 29 -

$$\frac{\cos A}{1 - \sin A} + \frac{\sin A}{1 - \cos A} + 1 = \frac{\sin A \cos A}{(1 - \sin A)(1 - \cos A)}$$

$$\text{LHS} = \frac{\cos A}{1 - \sin A} + \frac{\sin A}{1 - \cos A} + 1$$

$$\Rightarrow \frac{\cos A (1 - \cos A) + \sin A (1 - \sin A) + (1 - \sin A)(1 - \cos A)}{(1 - \sin A)(1 - \cos A)}$$

$$\Rightarrow \frac{\cos A - \cos^2 A + \sin A - \sin^2 A + 1 - \cos A - \sin A + \sin A \cos A}{(1 - \sin A)(1 - \cos A)}$$

$$\Rightarrow \frac{-(\cos^2 A + \sin^2 A) + 1 + \sin A \cos A}{(1 - \sin A)(1 - \cos A)}$$

$$\Rightarrow \frac{-(1) + 1 + \sin A \cos A}{(1 - \sin A)(1 - \cos A)} = \frac{-1 + 1 + \sin A \cos A}{(1 - \sin A)(1 - \cos A)}$$



$$\Rightarrow \frac{\sin A \cos A}{(1 - \sin A)(1 - \cos A)}$$

$$\text{LHS} = \text{RHS}$$

Hence Proved

Ans 30-

Given: ABCD is a quadrilateral

To prove:  $AB + CD = BC + AD$

Proof:

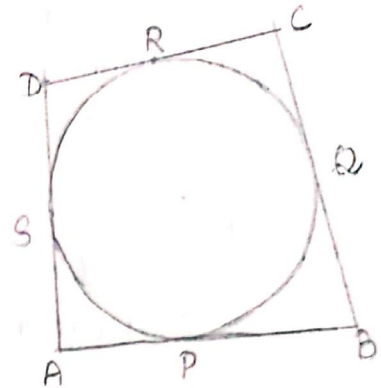
$$AP = AS$$

$$BP = BQ$$

$$CR = CQ$$

$$DR = DS$$

[tangent from same external point are equal]



Adding,

$$AP + BP + CR + DR = AS + DS + BQ + CQ$$

$$AB + CD = AD + BC$$

Hence, Proved.

Ans 31-

i. Total number of red coloured card = 26

Total number of card = 52

$$P(\text{red colored}) = \frac{\text{No. of outcomes}}{\text{Total no. of outcomes}} = \frac{26}{52} = \frac{1}{2}$$

ii. Total number of jack card = 4

Total number of card = 52

$$P(\text{jack}) = \frac{\text{No. of outcomes}}{\text{Total no. of outcomes}} = \frac{4}{52} = \frac{1}{13}$$

iii. Total number of red or jack card = 28

Total number of card = 52

$$P(\text{red or jack}) = \frac{\text{No. of outcomes}}{\text{Total no. of outcomes}} = \frac{28}{52} = \frac{7}{13}$$

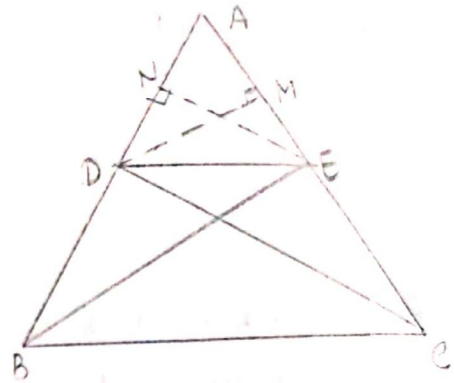
Ans 32-

Section-2

Given:  $\triangle ABC$ ,  $DE \parallel BC$

To prove:  $\frac{AD}{DB} = \frac{AE}{EC}$

Construction: Draw  $DM \perp AC$   
and  $EN \perp AB$ .



Proof:

$$\frac{\text{area}(\triangle ADE)}{\text{area}(\triangle DBE)} = \frac{\frac{1}{2} \times AD \times EN}{\frac{1}{2} \times DB \times EN} = \frac{AD}{DB} \quad \text{--- (1)}$$

$$\frac{\text{area}(\triangle AED)}{\text{area}(\triangle ECD)} = \frac{\frac{1}{2} \times AE \times DM}{\frac{1}{2} \times EC \times DM} = \frac{AE}{EC} \quad \text{--- (2)}$$

$$\text{area}(\triangle DBE) = \text{area}(\triangle ECD)$$

$$\frac{\text{area}(\triangle ADE)}{\text{area}(\triangle DBE)} = \frac{\text{area}(\triangle AED)}{\text{area}(\triangle ECD)}$$

[triangles are lying in the same base and same parallel line].

From eq (1) & (2)

$$\frac{AD}{DB} = \frac{AE}{EC}$$

Hence Proved

$DE \parallel BC$

$\Rightarrow \triangle ADE \sim \triangle ABC$

$$\frac{AD}{DB} = \frac{3}{4} \quad (\text{given})$$

Adding 1 both sides

$$\frac{AD}{DB} = \frac{3}{4} \Rightarrow \frac{DB}{AD} = \frac{4}{3}$$

$$\frac{DB+1}{AD} = \frac{4+1}{3}$$

$$\frac{DB+AD}{AD} = \frac{7}{3}$$

$$\frac{AB}{AD} = \frac{7}{3} \Rightarrow \frac{AD}{AB} = \frac{3}{7}$$

Now

$$\frac{AD}{AB} = \frac{DE}{BC} \Rightarrow \frac{DE}{BC} = \frac{3}{7}$$



Ans 33-

Let the speed of second train be  $x$  km/hr.

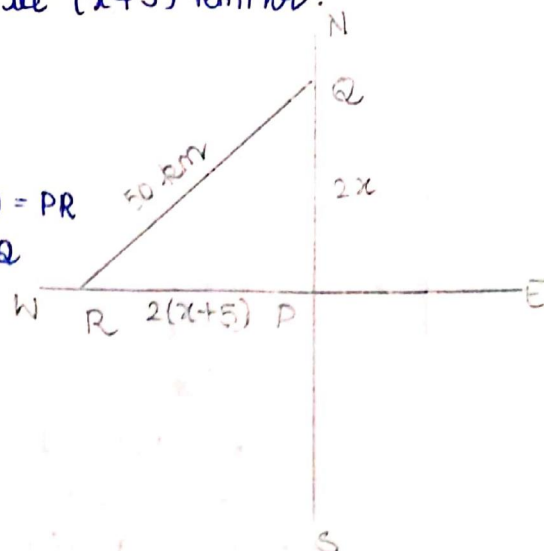
Let the speed of first train will be  $(x+5)$  km/hr.

Let point P be origin

Speed  $\times$  Time = Distance

Distance of first train =  $2(x+5) = PR$

Distance of second train =  $2x = PQ$



In  $\triangle QRP$

$$H^2 = P^2 + B^2$$

$$QR^2 = QP^2 + PR^2$$

$$(50)^2 = (2x)^2 + (2x+10)^2$$

$$2500 = 4x^2 + 4x^2 + 100 + 4x$$

Dividing equation by 4.

$$x^2 + x^2 + 25 + 10x = 625$$

$$2x^2 + 10x - 600 = 0$$

$$x^2 + 5x - 300 = 0$$

$$x^2 + 20x - 15x - 300 = 0$$

$$x(x+20) - 15(x+20) = 0$$

$$(x-15)(x+20) = 0$$

$$x = 15, x \neq -20$$

Hence, the actual speed of second train =  $15$  km/hr.

and the speed of first train =  $(x+5)$  km/hr  
=  $(15+5)$  km/hr  
=  $20$  km/hr.

'Or'

Let the time taken by the faster pipe to fill the cistern be  $x$  min.

Let the time taken by the slower pipe be  $(x+3)$  minutes.

The portion of cistern filled by the pipe in 1 minute is  $\frac{1}{x}$ .

The portion of cistern filled by the faster pipe in  $\frac{40}{13}$  minutes is  $\frac{40}{13x}$ .

The portion of cistern filled by the slower pipe in  $\frac{40}{13}$  minutes is  $\frac{40}{13(x+3)}$ .

As the cistern is filled fully in  $\frac{40}{13}$  minutes.

then,

$$\Rightarrow \frac{40}{13x} + \frac{40}{13(x+3)} = 1$$

$$\Rightarrow \frac{1}{x} + \frac{1}{x+3} = \frac{13}{40}$$

$$\Rightarrow \frac{x+3+x}{x^2+3x} = \frac{13}{40}$$

$$\Rightarrow \frac{2x+3}{x^2+3x} = \frac{13}{40}$$

$$\Rightarrow 40(2x+3) = 13(x^2+3x)$$

$$\Rightarrow 13x^2 - 41x - 120 = 0$$

$$\Rightarrow 13x^2 - 65x + 24x - 120 = 0$$

$$\Rightarrow 13x(x-5) + 24(x-5) = 0$$

$$(13x+24)(x-5) = 0$$

$$x = -\frac{24}{13}, \quad x = 5$$

$\therefore x$  can not be a negative

Therefore, the faster pipe will fill the cistern in 5 minutes and the slower pipe will fill the cistern in 8 minutes.

Ans 34- Diameter of sphere (d) = 12 cm

Radius of sphere (r) = 6 cm

Water level in the vessel rises by  $3\frac{5}{9}$  hours =  $\frac{32}{9}$  hours

Volume of sphere = volume of water rise in cylindrical vessel

$$\frac{4}{3} \pi \times (6)^3 = \pi r^2 h$$

$$\frac{4}{3} \times \pi \times (6)^3 = \pi \times r^2 \times \frac{32}{9}$$

$$288 = \frac{32 r^2}{9}$$

$$2592 = 32 r^2$$

$$\frac{2592}{32} = r^2$$

$$r^2 = 81$$

$$r = 9$$

Hence, the diameter of the cylindrical vessel = 18 cm



'031'

Ans  $\Rightarrow$

$$\text{Diameter (d) of the graphite cylinder} = 1\text{mm} = \frac{1}{10}\text{ cm}$$

$$\text{Radius (r) of cylinder} = \frac{1}{20}\text{ cm}$$

$$\text{Length of the graphite cylinder} = 10\text{ cm}$$

$$\begin{aligned}\text{Volume of the graphite cylinder} &= \pi r^2 h \\ &= \left( \frac{22}{7} \times \frac{1}{20} \times \frac{1}{20} \times 10 \right) \text{ cm}^3\end{aligned}$$

$$\begin{aligned}\text{Weight of graphite} &= \text{Volume} \times \text{specific gravity} \\ &= \left( \frac{22}{7} \times \frac{1}{20} \times \frac{1}{20} \times 10 \times 2.1 \right) \text{ gm} \\ &= 0.165 \text{ gm}\end{aligned}$$

$$\text{Diameter of pencil} = 7\text{mm} = \frac{7}{10}\text{ cm}$$

$$\text{Radius (R) of pencil} = \frac{7}{20}\text{ cm}$$

$$\text{Length of pencil} = 10\text{ cm}$$

$$\text{Volume of pencil} = \left( \frac{22}{7} \times \frac{7}{20} \times \frac{7}{20} \times 10 \right) \text{ cm}^3$$

$$\text{Volume of wood} = \left( \frac{22}{7} \times \frac{7}{10} \times \frac{7}{10} \times 10 - \frac{22}{7} \times \frac{1}{20} \times \frac{1}{20} \times 10 \right) \text{ cm}^3$$

$$\begin{aligned}\text{Volume of wood} &= \frac{22}{7} \times \frac{1}{20} \times \frac{1}{20} \times 10 (7 \times 7 - 1) \text{ cm}^3 \\ &= \left( \frac{11}{7} \times \frac{1}{20} \times 48 \right) \text{ cm}^3\end{aligned}$$

$$\text{Weight of wood} = \left( \frac{11}{7} \times \frac{1}{20} \times 48 \times 0.7 \right) \text{ gm}$$

$$= 2.64 \text{ gm}$$

$$\text{Total weight} = (2.64 + 0.165) \text{ gm} = 2.805 \text{ gm}$$

Ans 35.

C.I	$f_i$	$x_i$	$f_i x_i$
10-30	90	20	1800
30-50	$f_1$	40	$40f_1$
50-70	30	60	1800
70-90	$f_2$	80	$80f_2$
90-110	40	100	4000

Total frequency = 200

$$f_1 + f_2 = 40 \text{ --- (1)}$$

$$\text{Mean} = 50$$

$$\text{Mean} = \frac{\sum f_i x_i}{\sum f_i}$$

$$50 = \frac{7600 + 40f_1 + 80f_2}{200}$$

$$\Rightarrow 40f_1 + 80f_2 = 2400$$

$$\Rightarrow f_1 + 2f_2 = 60 \text{ --- (2)}$$

By elimination method,

$$f_2 = 20$$

putting  $f_2 = 20$  in eq (1)

$$f_1 + f_2 = 40$$

$$f_1 + 20 = 40$$

$$f_1 = 20$$

Therefore, the value of  $f_1$  and  $f_2$  is 20 & 20

### Section-E

Ans 36- i). AP  $\Rightarrow 4, 8, 12, \dots, 27$   
 $a = 4$   $d = 4$

Middlemost flag is 14<sup>th</sup> flag

For placing fourteenth flag and return her initial position =  $26 + 26 = 52\text{m}$

(iii). Here  $S_{13} = \frac{13}{2} [2 \times 4 + (13-1)4]$   
 $= \frac{13}{2} (8 + 48) = \frac{13}{2} \times 56 = 364$

Distance travelled to fix 13 flag to the left of A = 364m



Similarly distance travelled to find remaining  
13 to right of A = 364m  
Total distance = 364 + 364 = 728m.

OR  
Total steps she needed to cover 728m  
will be  $728 \times 3 = 2184$  steps

(ii) She completed the task in 6 minutes  
Total distance travelled = 728m  
 $T = \frac{D}{S} \Rightarrow S = \frac{D}{T} = \frac{728}{6} = 2.02 \text{ m/s}$   
Her speed will be 2.02 m/s

Ans 37-

Coordinates :

A(3, 2) B(5, 6) C(8, 1)

$$D \Rightarrow \left[ \frac{3+5}{2}, \frac{2+6}{2} \right]$$

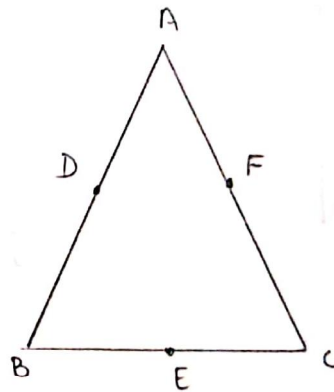
$$\Rightarrow \left( \frac{8}{2}, \frac{8}{2} \right) = (4, 4)$$

$$F \Rightarrow \left[ \frac{3+8}{2}, \frac{2+1}{2} \right]$$

$$\Rightarrow \left( \frac{11}{2}, \frac{3}{2} \right)$$

$$E \Rightarrow \left[ \frac{5+8}{2}, \frac{6+1}{2} \right]$$

$$\Rightarrow \left( \frac{13}{2}, \frac{7}{2} \right)$$



i).  $AD = \sqrt{(x_2 + x_1)^2 + (y_2 + y_1)^2}$   
 $= \sqrt{(4-3)^2 + (4-2)^2}$   
 $= \sqrt{1+4} = \sqrt{5}$

ii).  $EF = \sqrt{\left(\frac{13}{2} - \frac{11}{2}\right)^2 + \left(\frac{7}{2} - \frac{3}{2}\right)^2}$   
 $= \sqrt{\left(\frac{2}{2}\right)^2 + \left(\frac{4}{2}\right)^2}$   
 $= \sqrt{(1)^2 + (2)^2} = \sqrt{1+4}$   
 $= \sqrt{5}$

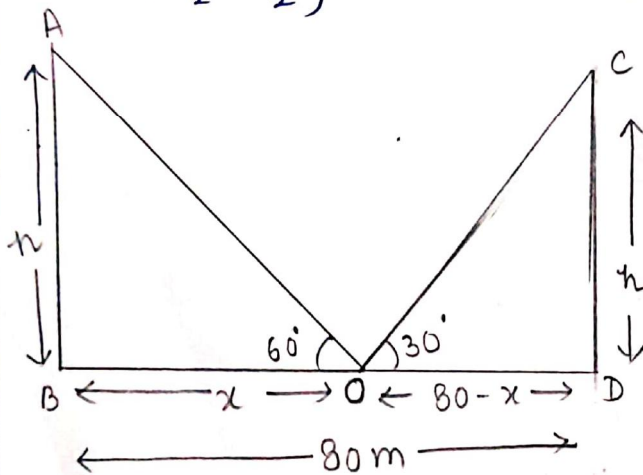
iii

$D = (4, 4)$   
 $E = \left(\frac{13}{2}, \frac{7}{2}\right)$   
 $F = \left(\frac{11}{2}, \frac{3}{2}\right)$

OR

Point of Intersection of  
 AE, BF & CD.  
 will be centroid of  $\triangle ABC$   
 $= \left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3}\right) = \left(\frac{3+5+8}{3}, \frac{2+6+1}{3}\right)$   
 $= \left(\frac{16}{3}, 3\right)$

Ans 38-



i). AB is closer. Because angle of elevation is high

ii).

In  $\triangle ABO$

$$\frac{AB}{BO} = \tan 60^\circ$$

$$\frac{h}{x} = \sqrt{3}$$

$$h = \sqrt{3}x$$

In  $\triangle CDO$

$$\frac{CD}{DO} = \tan 30^\circ$$

$$\frac{h}{80-x} = \frac{1}{\sqrt{3}}$$



$$\sqrt{3}(x\sqrt{3}) = 80 - x$$

$$3x = 80 - x$$

$$4x = 80$$

$$x = 20$$

$$BO = 20 \text{ m}$$

$$DO = 80 - 20 \\ = 60 \text{ m}$$

iii.

$$\text{Height of pole} \Rightarrow \tan 60^\circ = \frac{AB}{BO}$$

$$\sqrt{3} = \frac{h}{x}$$

$$x\sqrt{3} = h$$

$$h = 20\sqrt{3} \text{ m}$$

'OM'

$$\text{Height of pole} = 20\sqrt{3} \text{ m}$$

$$\text{Distance of point} = 20 \text{ m}$$

$$\text{Ratio} = \frac{20\sqrt{3}}{20} = \frac{\sqrt{3}}{1} = \sqrt{3}:1$$